



Optical Combs in the mid-IR: Frequency Divide-and-Conquer Approach



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Beginning of the Laser Era in the USSR: 1939-1976

Early Soviet Papers on Quantum Electronics

Beginning of the Laser Era in the USSR

a special reprint collection for [LaserFest](http://www.opticsinfobase.org/laserfest)



The 50th anniversary of the laser has stimulated worldwide interest in the history of quantum electronics. This special collection, "Beginning of the Laser Era in the USSR," presents early Soviet pioneering works that had a significant impact on laser science and quantum electronics. Several of the papers have never been published in English and were not generally available outside the USSR.

[http://www.opticsinfobase.org/
laserfest/laserfest-soviet.cfm](http://www.opticsinfobase.org/laserfest/laserfest-soviet.cfm)

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Anti -second harmonic generation

$\omega \rightarrow 2\omega$ second harmonic generation

$\omega \rightarrow \omega/2$ sub-harmonic generation



Standing on shoulders of giants



Sergei Akhmanov
(Moscow State Univ.)

Prior work on
microwave degenerate
parametric oscillators



Lev Kulevsky
(Lebedev Inst. Moscow)

Introduced me to
nonlinear optics

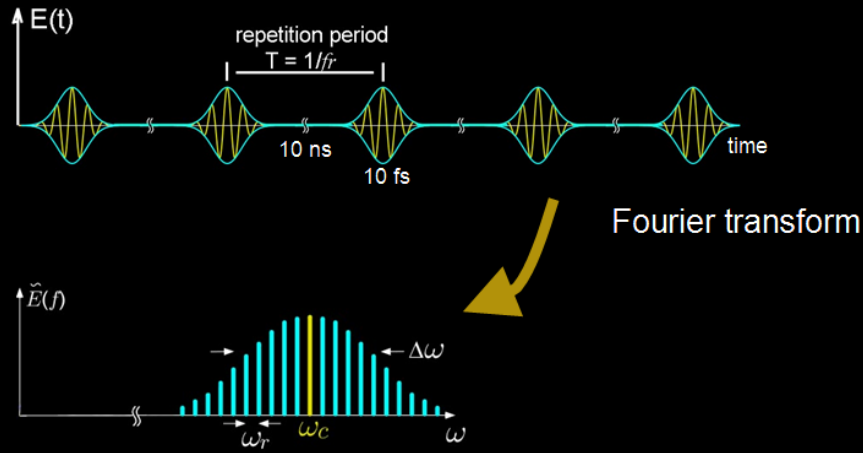


Robert Byer
(Stanford University)

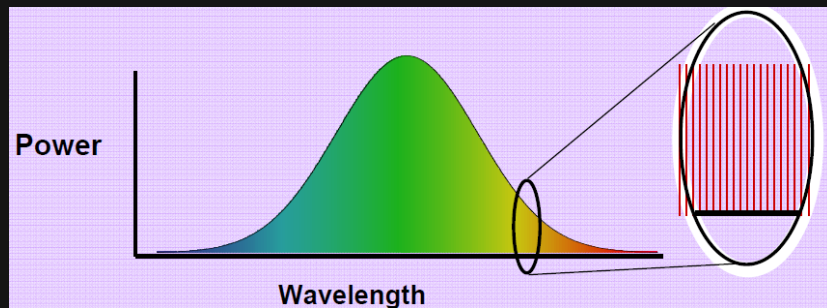
Prior work on CW
degenerate OPO



What are frequency combs ?



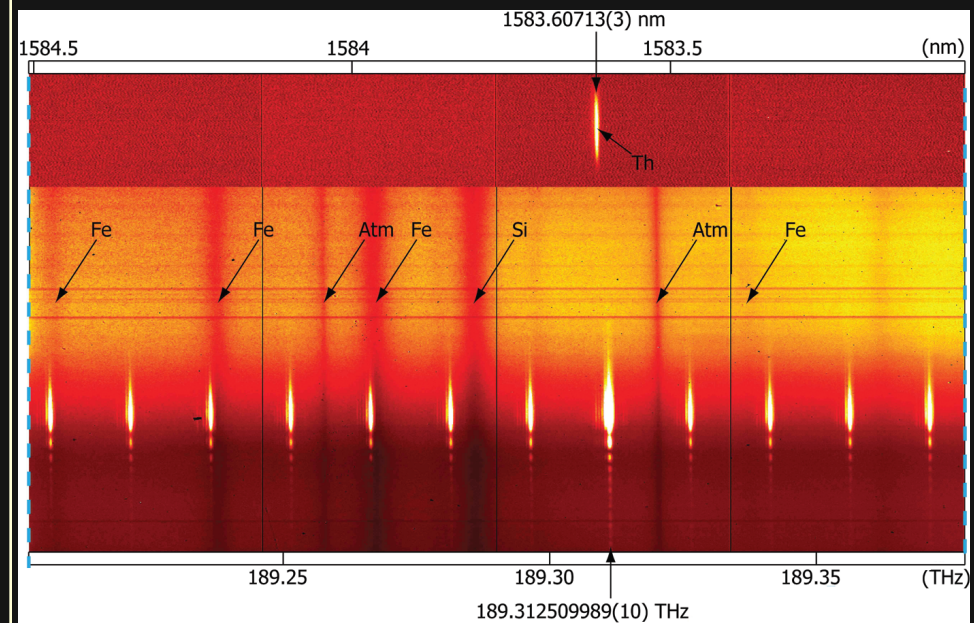
Regularly spaced train of short (fs) pulses corresponds to a comb in the frequency domain



Spectra of the solar photosphere near $1.5\mu\text{m}$ overlaid by a Laser Frequency Comb with 15-GHz mode spacing

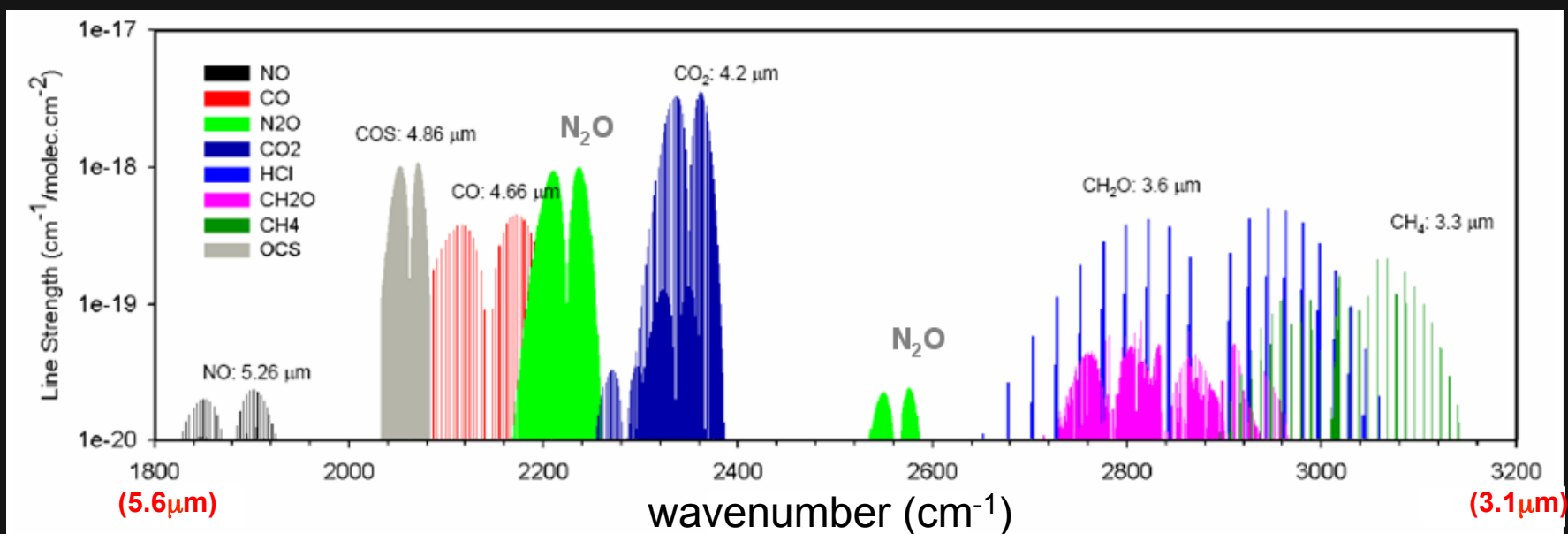
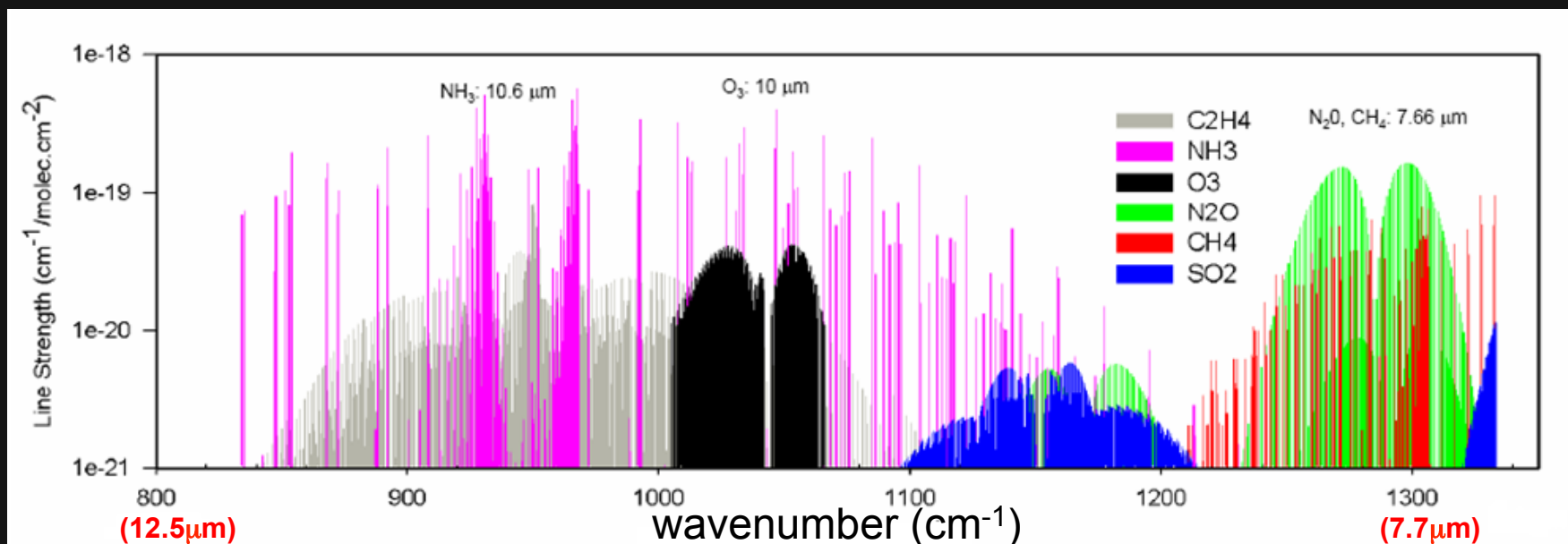
Steinmetz et al. *Science* **321**, 1335 (2008)

Theodor W. Hänsch and John L. Hall
2005 Nobel Prize in Physics



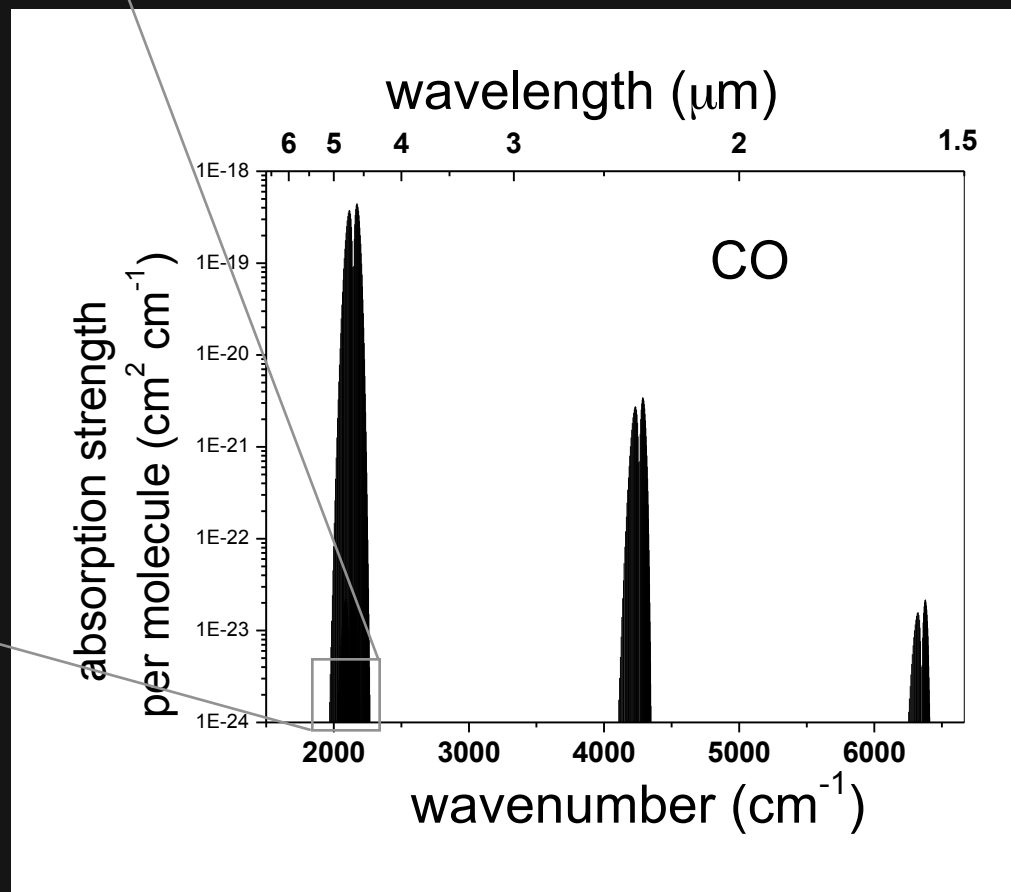
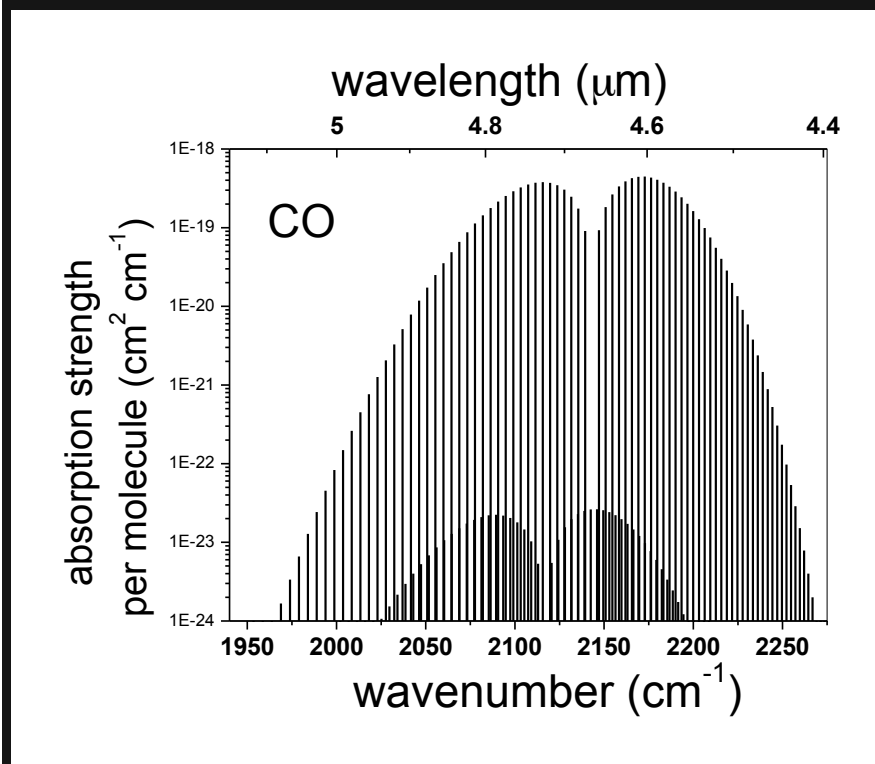


Molecular spectra in the “signature” mid-IR spectral range (3-12 μm)



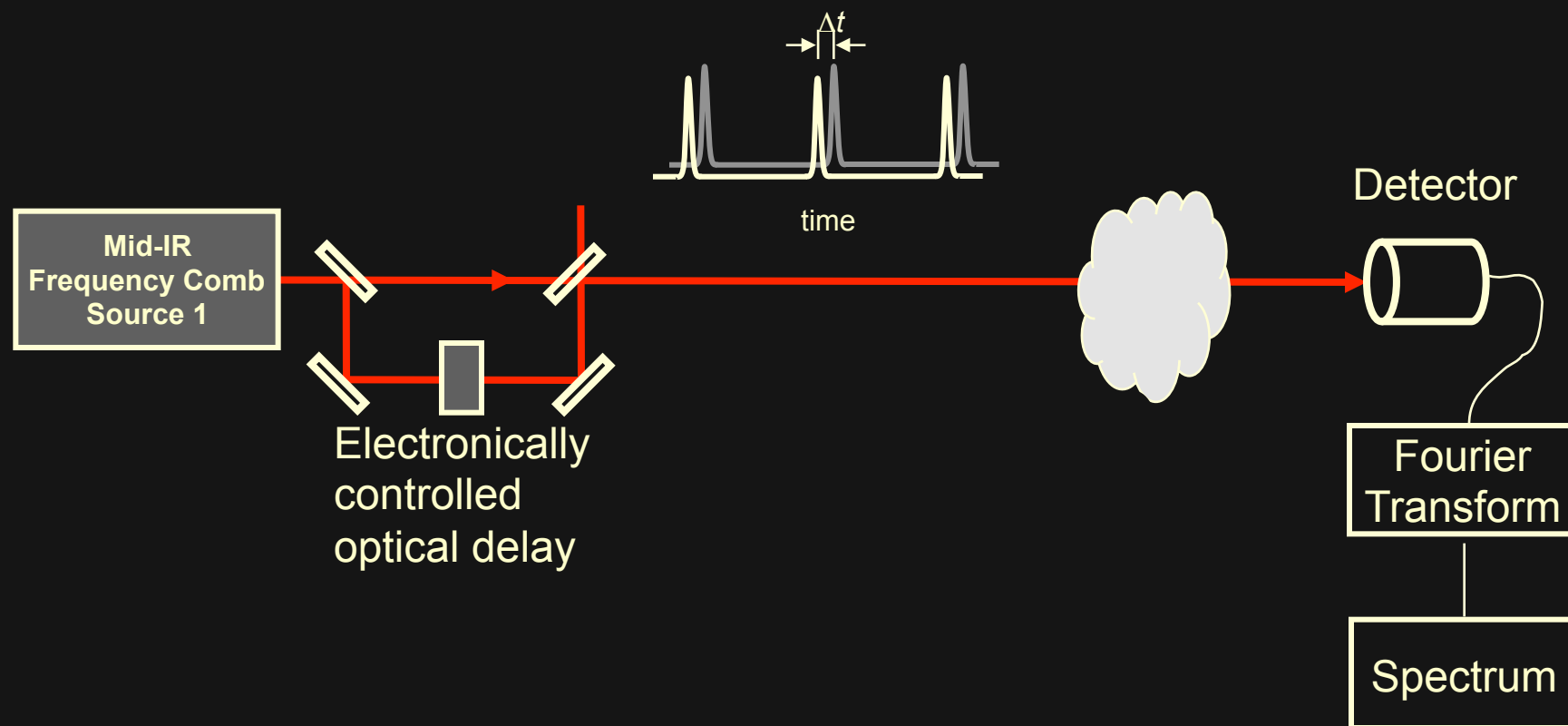


CO molecule spectrum





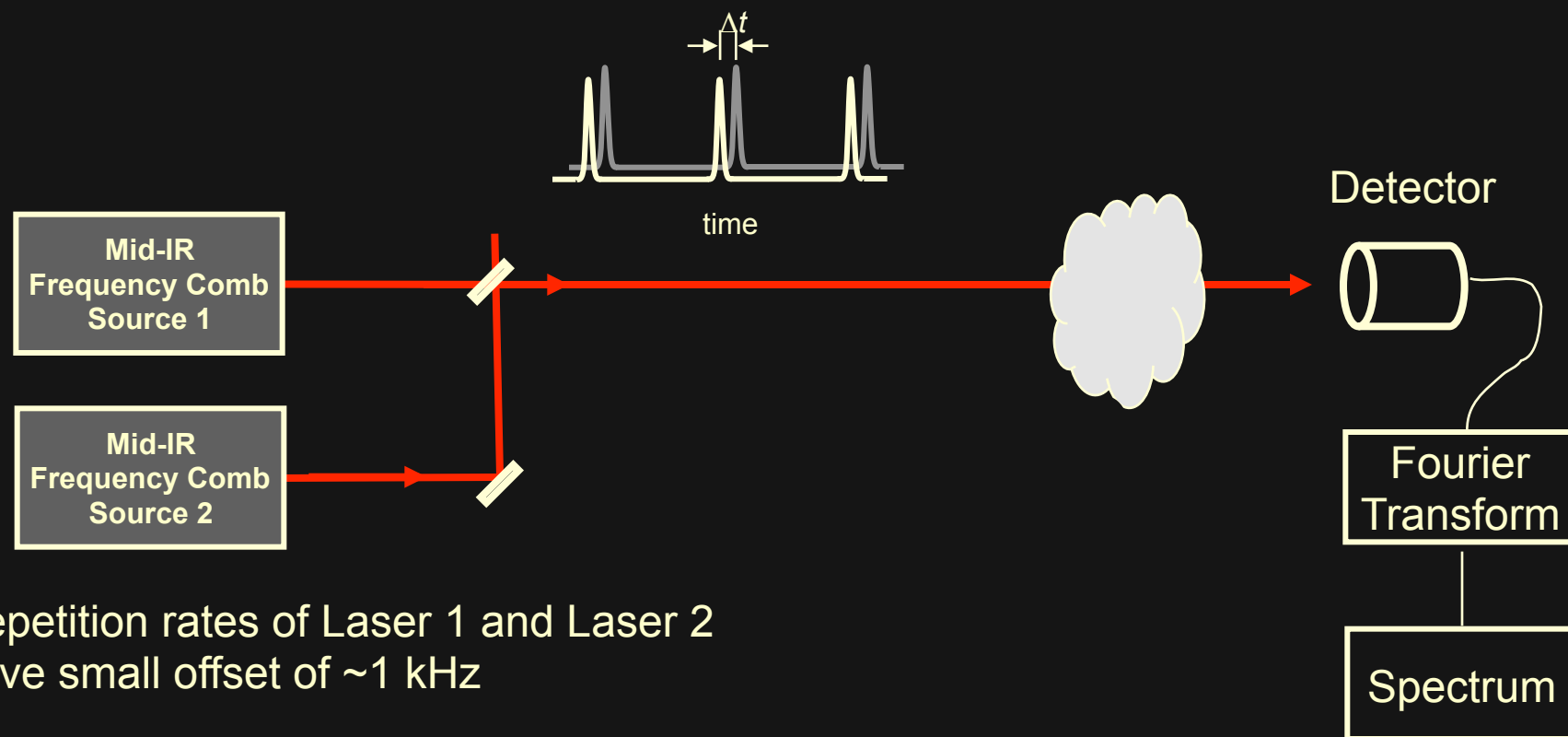
Comb Fourier Transform Spectroscopy





Dual-Comb Fourier Transform Spectroscopy

Schliesser, Brehm, Keilmann, Opt. Express 13, 9029 (2005)



Repetition rates of Laser 1 and Laser 2
have small offset of ~ 1 kHz

Up to 1000 spectra/sec
Resolution ~ 100 MHz (0.003 cm^{-1})



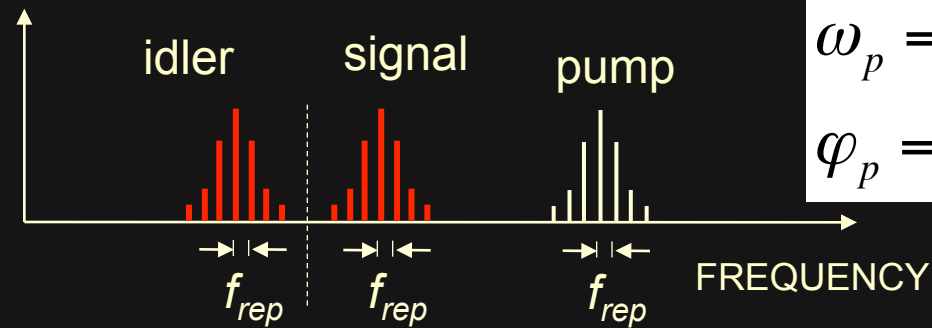
Frequency combs in the mid-IR

- **Direct laser sources, e.g. Cr²⁺: ZnSe**
Sorokin et al., Opt. Express 15, 16540 (2007)
- **Supercontinuum from optical fibers**
Washburn et al., Opt. Lett. 29, 250-252 (2004)
- **Optical parametric oscillators**
Sun, Gale, Reid. Opt. Lett. 32, 1414-1416 (2007).
Adler et al. Opt. Lett. 34, 1330-1332 (2009).
- **Difference frequency generation**
Erny, Moutzouris, Biegert, Kühlke, Adler, Leitenstorfer, Keller, Opt. Lett. 32, 1138-1140 (2007)
- **Optical rectification**
Keilmann, Gohle, Holzwarth, Opt. Lett. 29, 1542-1544 (2004)
- **Microresonators**
Wang, Herr, Pascal Del'Haye, Schliesser, Holzwarth, Haensch, Picque, Kippenberg,
Post-Deadline, CLEO -2011



Degenerate $\chi^{(2)}$ sync-pumped OPO

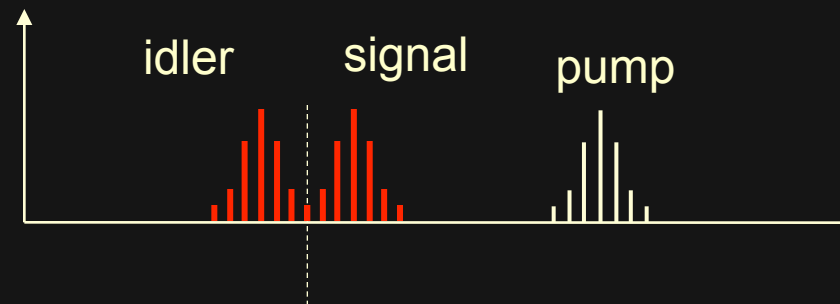
non-degenerate OPO



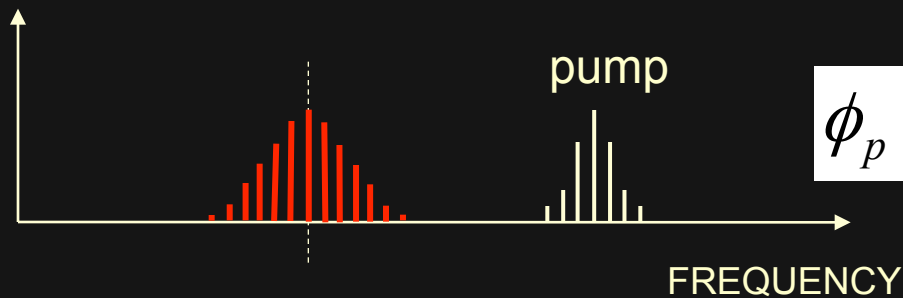
$$\omega_p = \omega_s + \omega_i$$

$$\varphi_p = \varphi_s + \varphi_i + \pi / 2$$

partly degenerate OPO



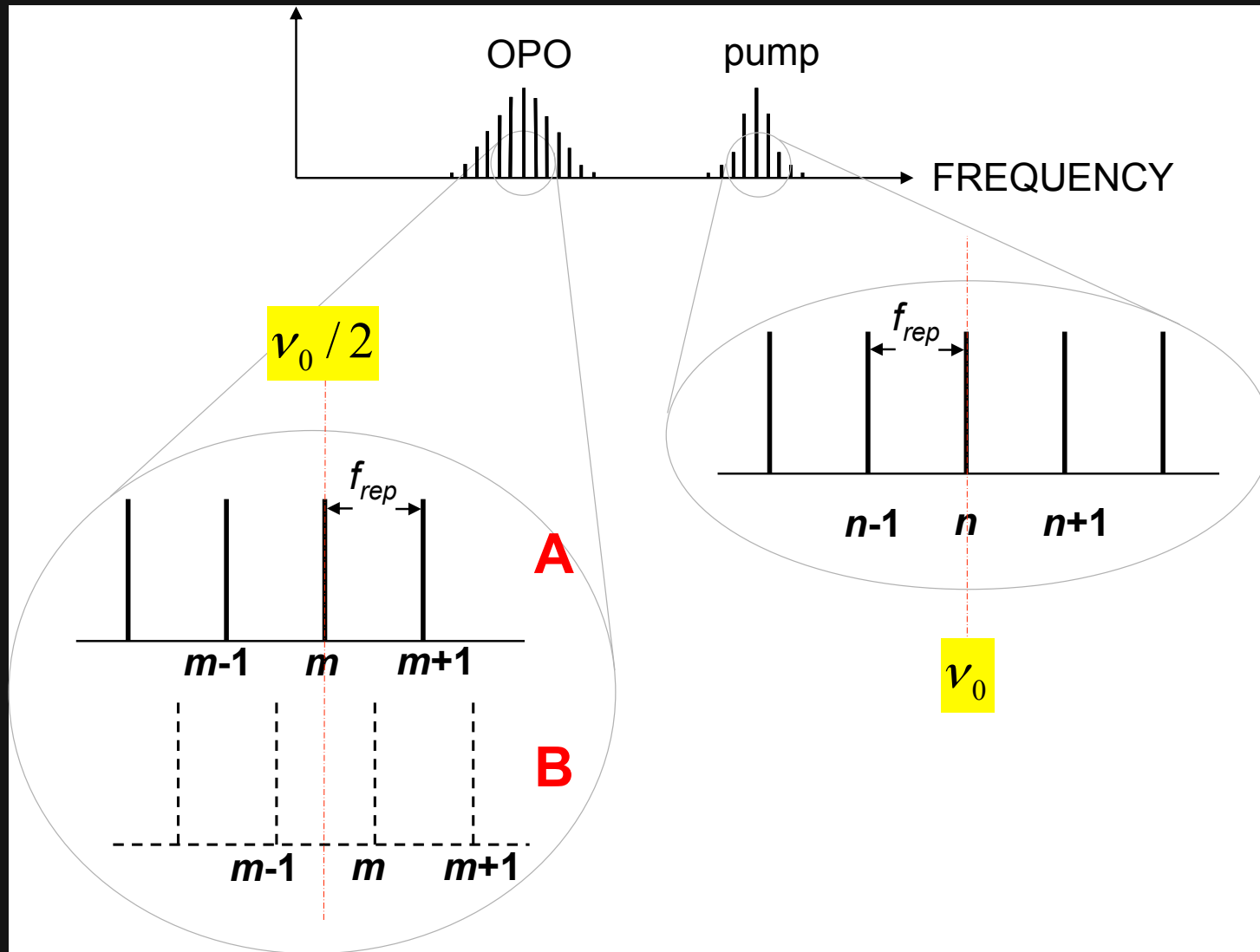
degenerate OPO



$$\phi_p = 2\phi_{s,i} + \pi / 2$$

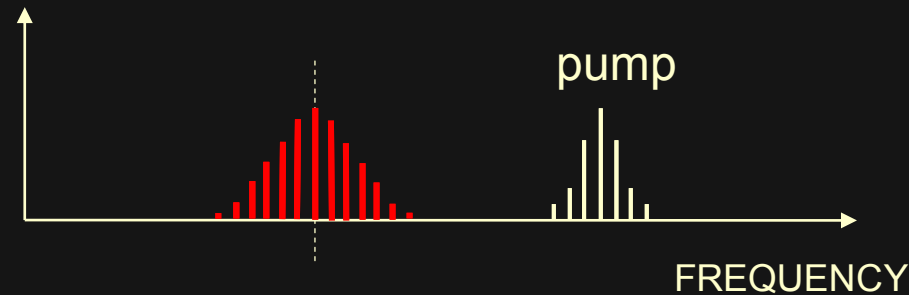


Longitudinal modes of the sync-pumped degenerate OPO





Degenerate synch-pumped OPO



1. **Large acceptance bandwidth at degeneracy**

$$\sim \beta_2^{-1/2} \quad (\beta_2 = d^2 k / d\omega^2)$$

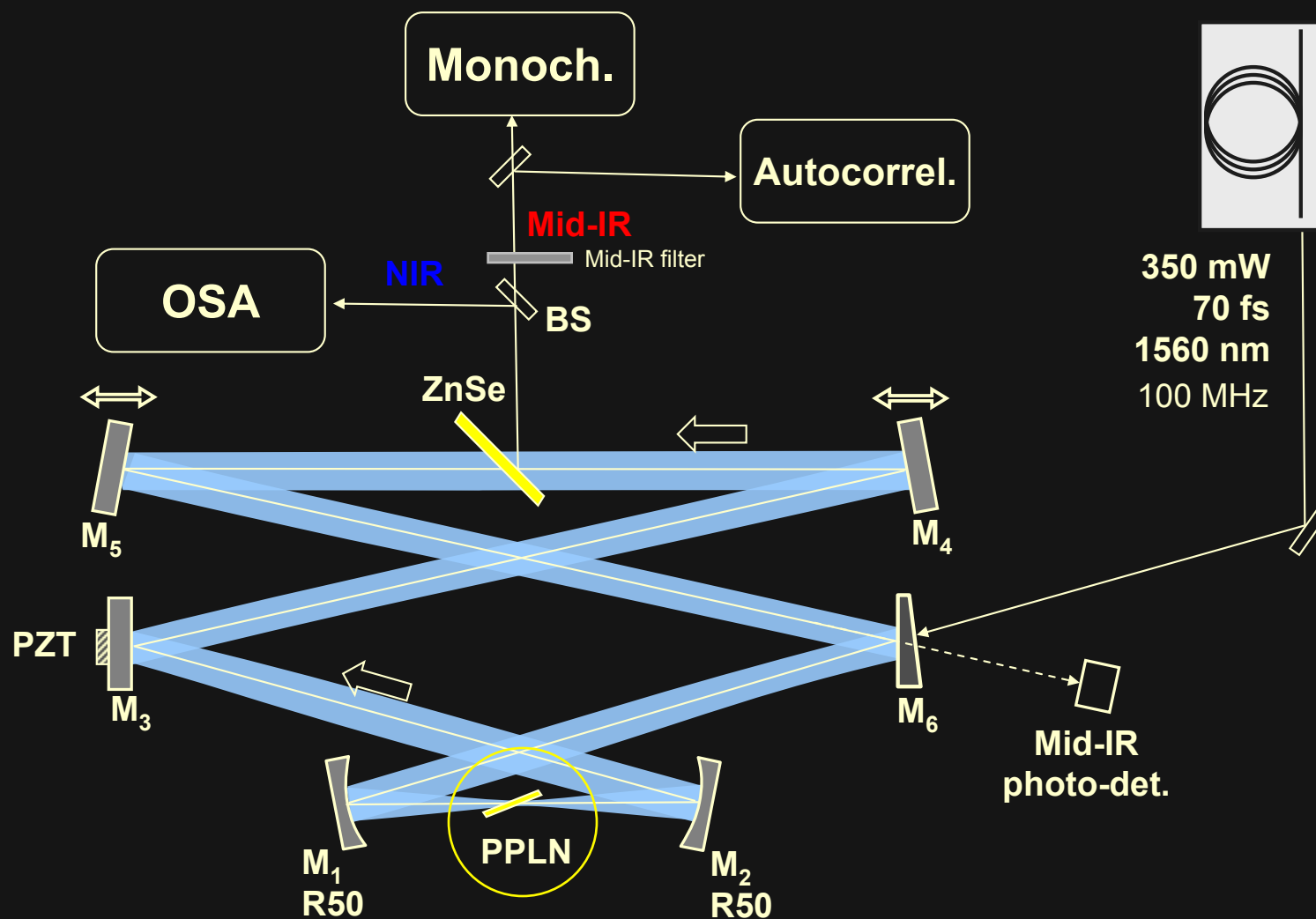
$$\sim \beta_4^{-1/4}, \text{ if } \beta_2 = 0 \quad (\beta_4 = d^4 k / d\omega^4)$$

2. **Double resonance $\rightarrow$ low pump threshold**

3. **OPO is phase- and frequency locked to the pump laser**

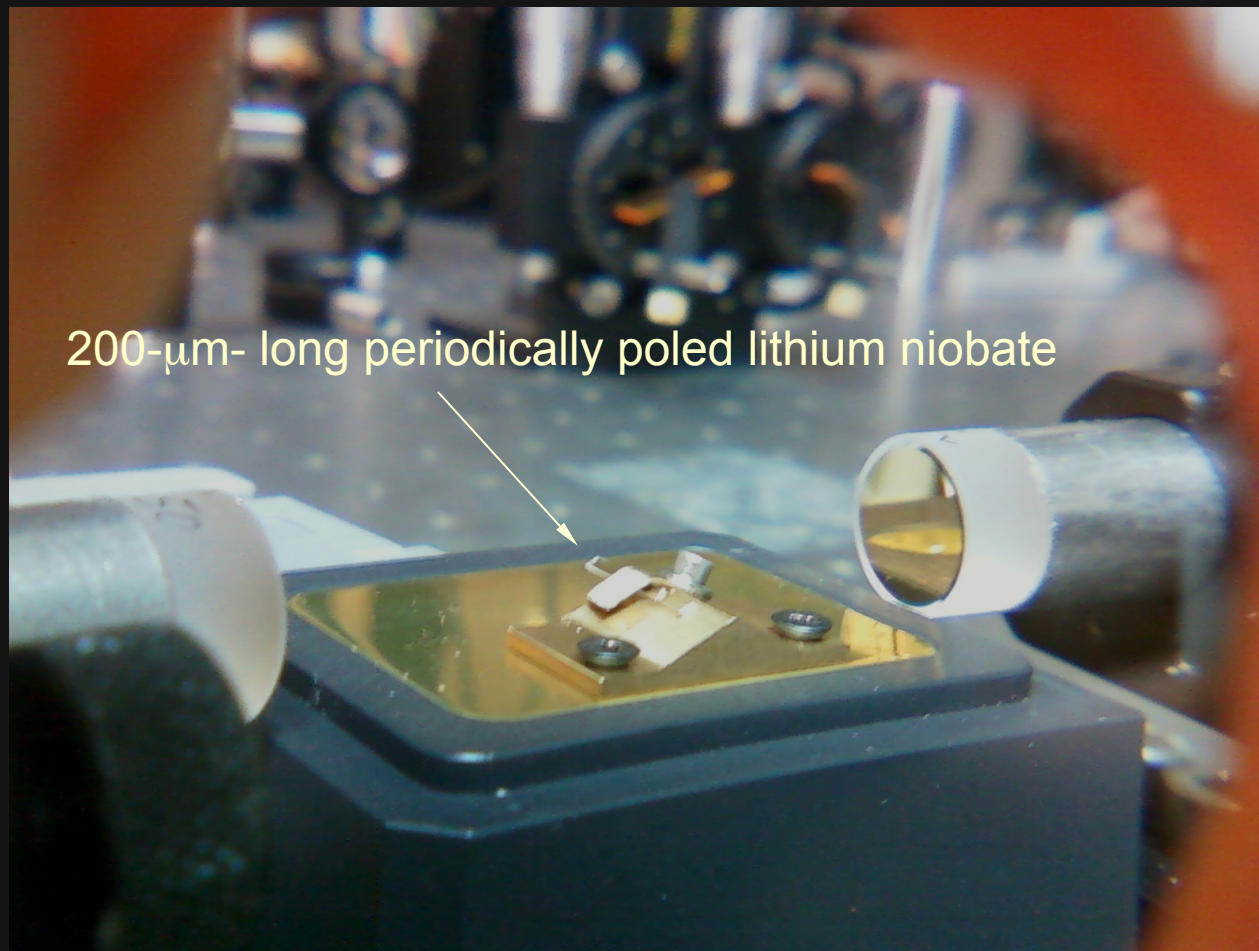


Mid-IR subharmonic OPO setup





“OPO engine”



200- μm - long periodically poled lithium niobate

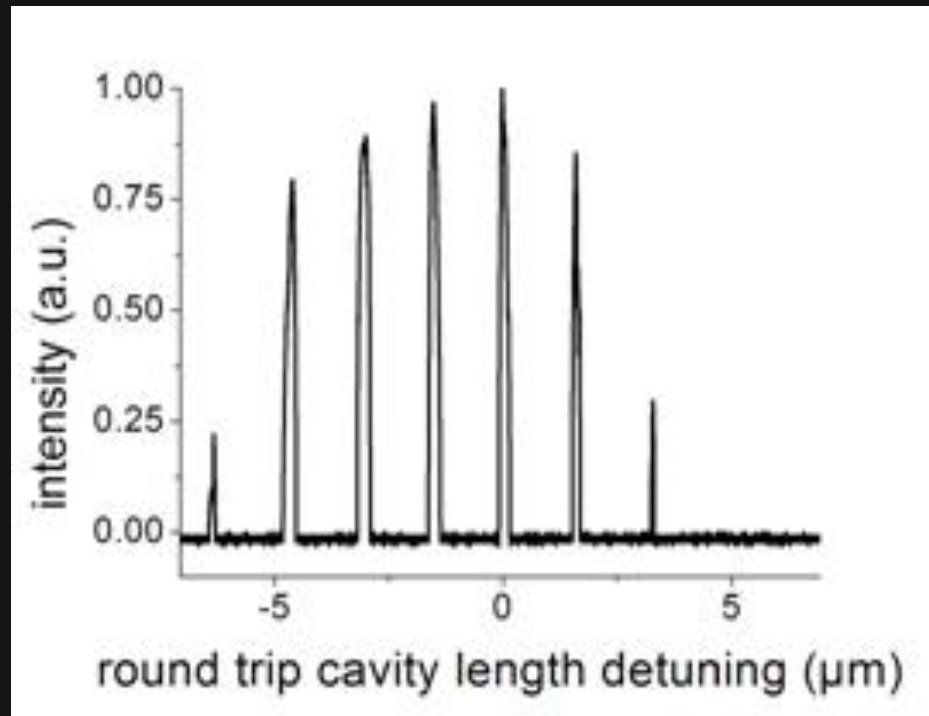
PPLN crystal:

500 μm (14 periods)
or
200 μm (6 periods)

Brewster-cut

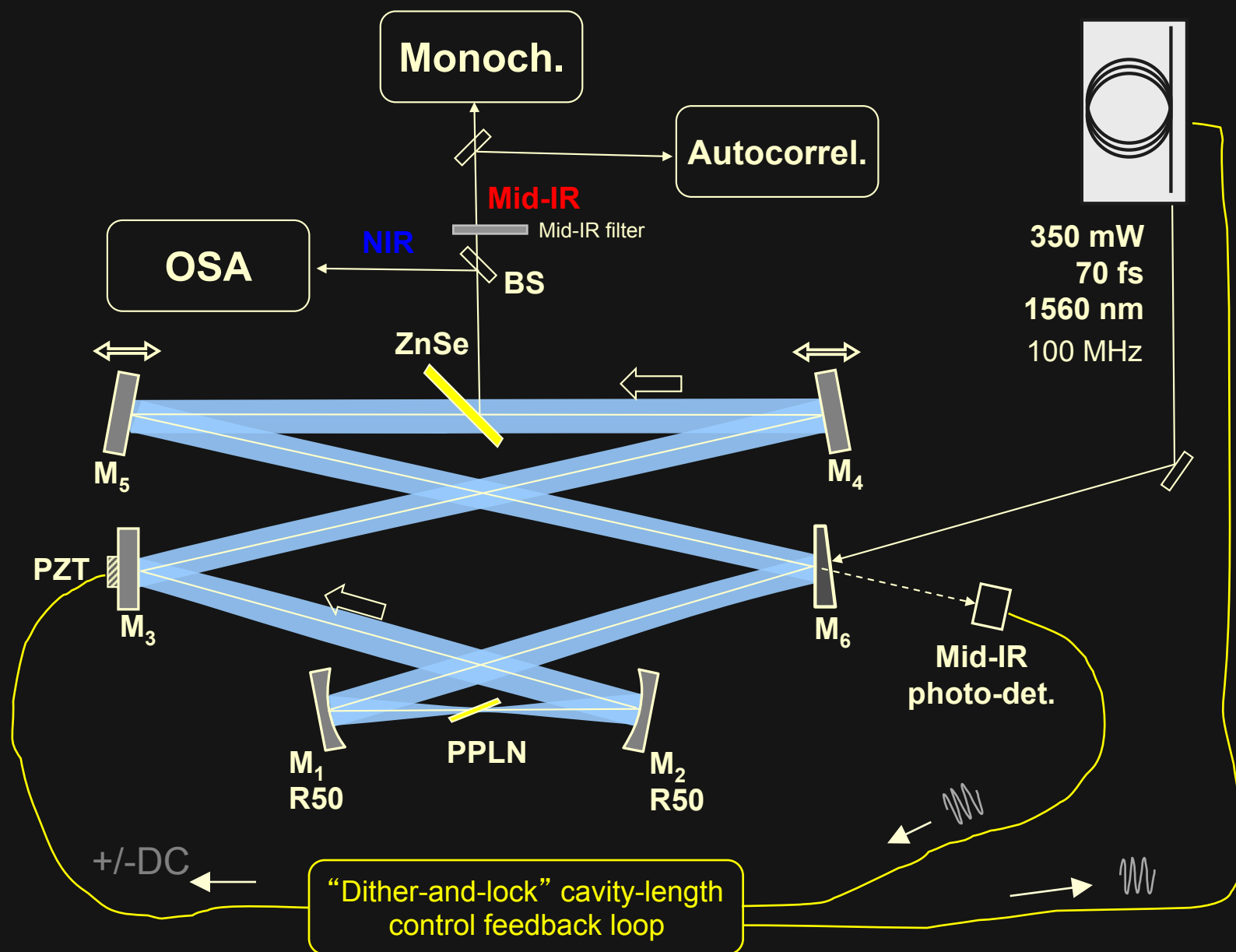


OPO oscillation occurs at several discrete cavity lengths
Can be stabilized at each of those peaks





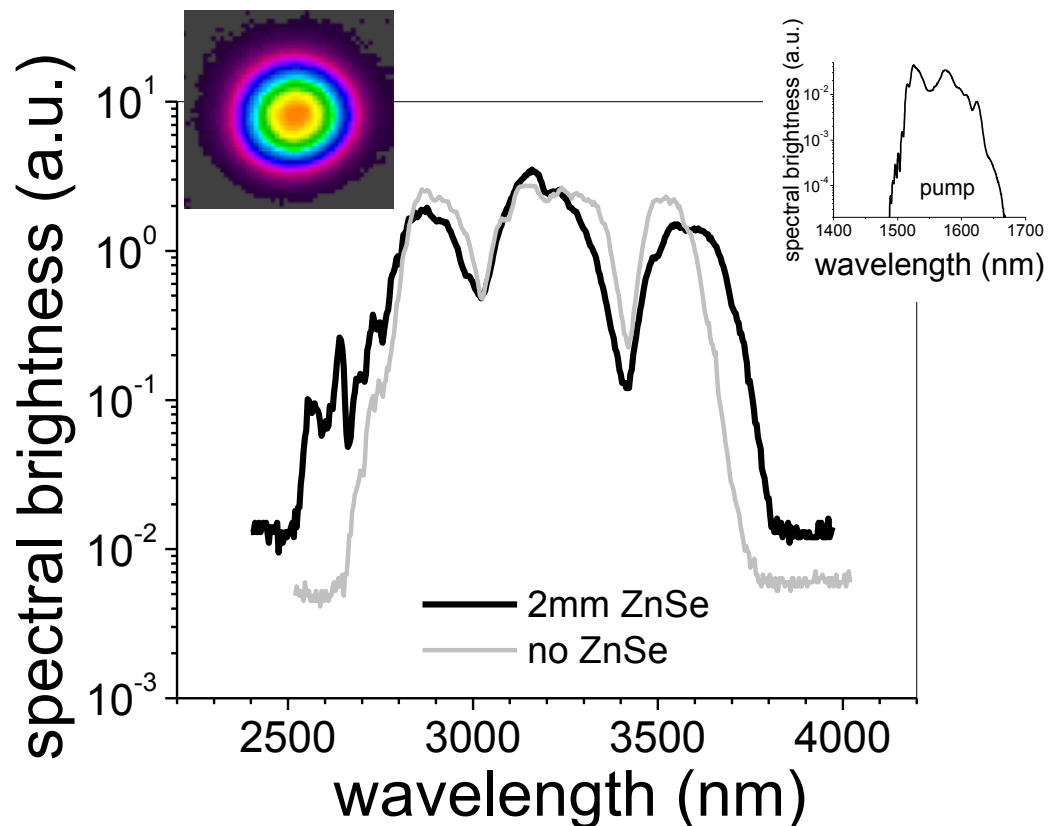
Mid-IR subharmonic OPO setup



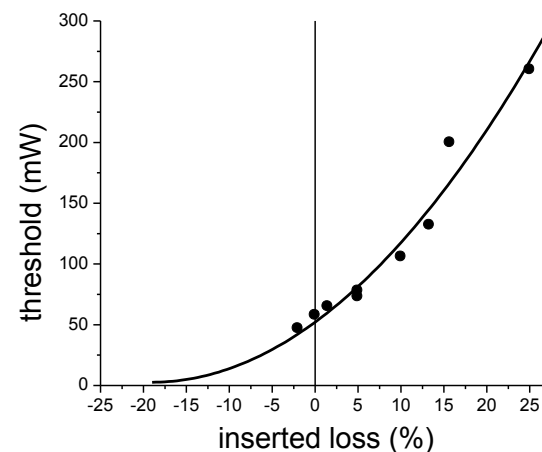


OPO main features

Spectrum: Monochromator



Threshold $\sim (\text{loss})^2$



Pump threshold 9 mW

Pump depletion 80-83%

Outcoupled power 60 mW

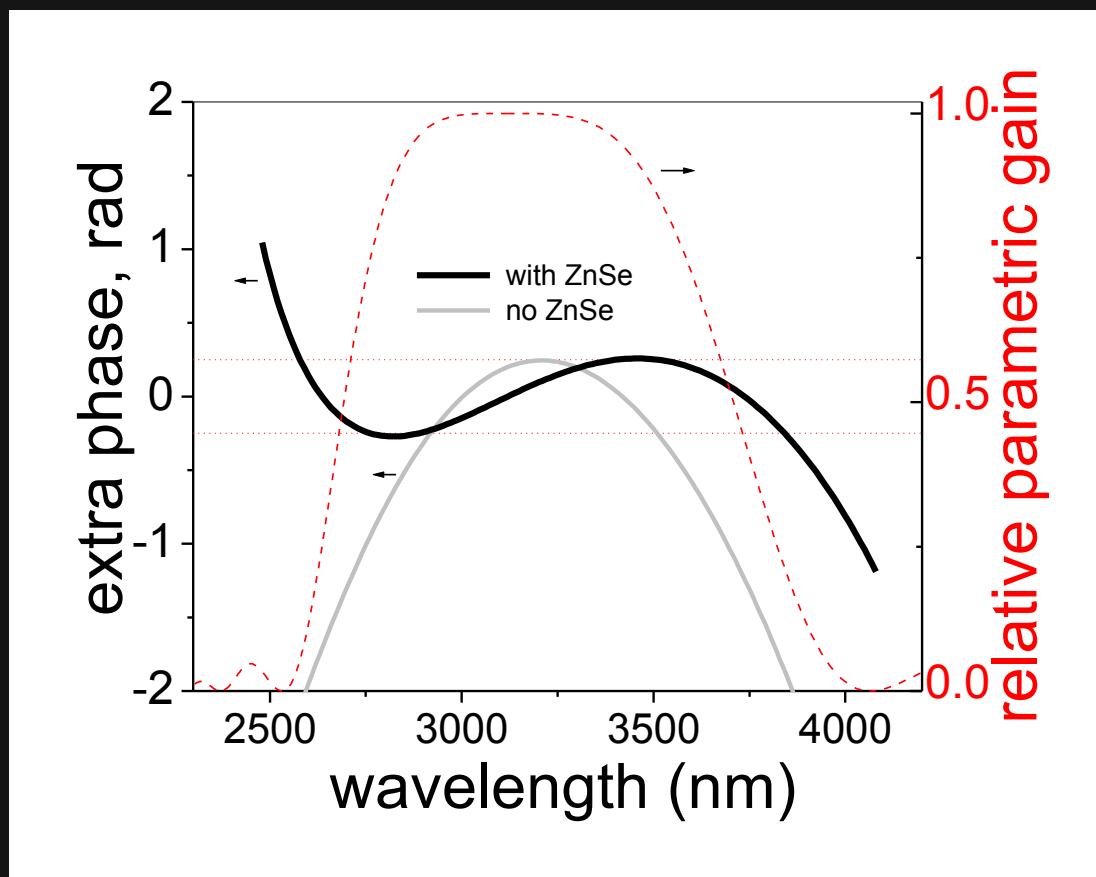
Bandwith 2500-3900 nm (2/3 octaves)

**Can support 3-cycle pulses
at $\sim 3 \mu\text{m}$**

Intracavity power 1.2W



What limits the comb spectral width ?



Computed extra phase accumulated per cavity roundtrip due to the dispersion of 0.5-mm PPLN plus mirrors (gray curve) and (black curve) with ZnSe added for dispersion compensation.

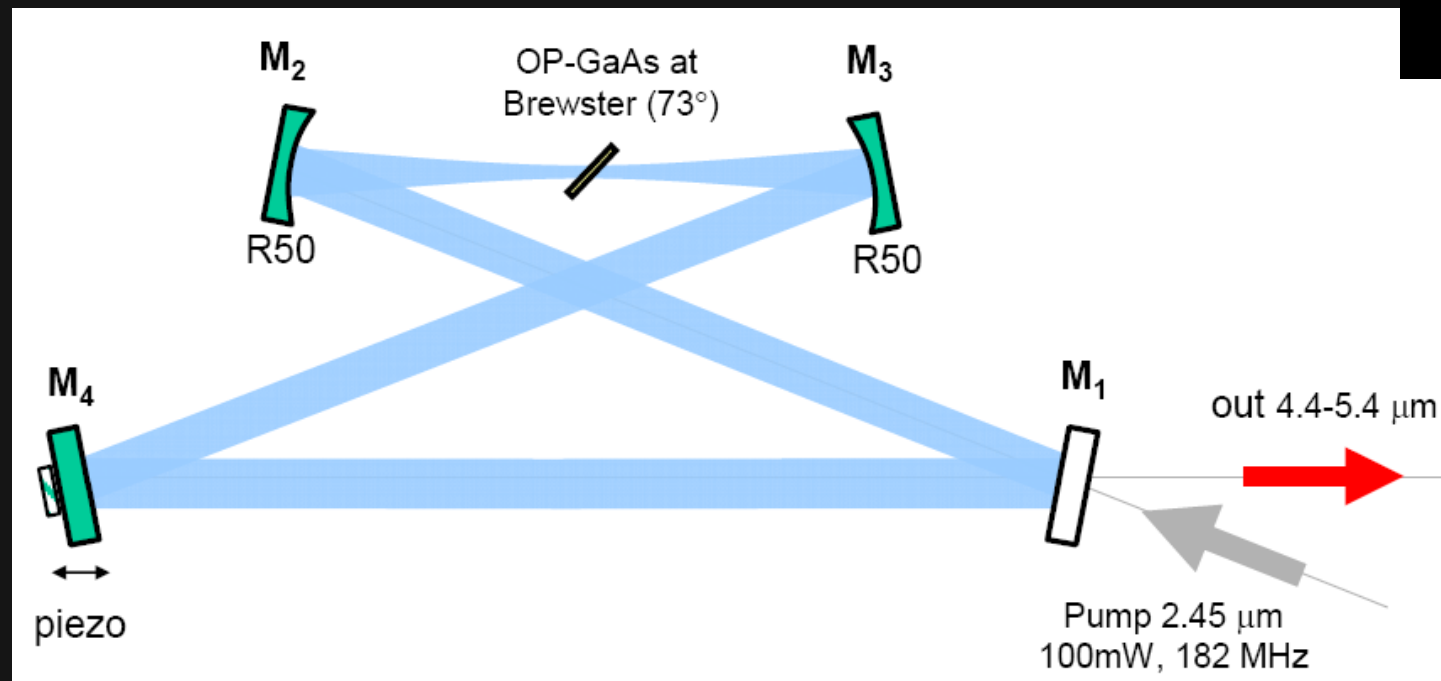
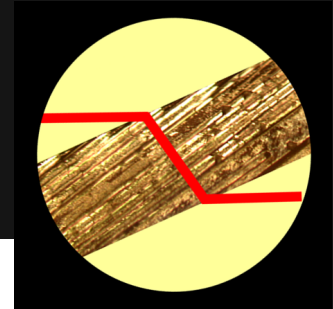


Results with orientation-patterned GaAs pumped at $2.45\text{ }\mu\text{m}$

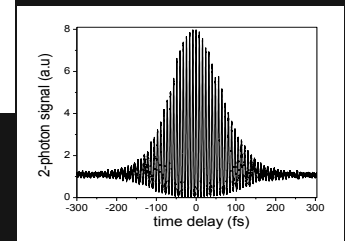
4.4-5.4 μm frequency comb was produced in a subharmonic OP-GaAs OPO pumped by a femtosecond $\text{Cr}^{2+}:\text{ZnSe}$ laser at $2.45\text{ }\mu\text{m}$

Pump threshold 40mW

OP-GaAs : 500- μm -long
QPM period: 92 μm
Beam k -vector: along [110]
Polarization: along [111]



$\tau \approx 100\text{fs}$

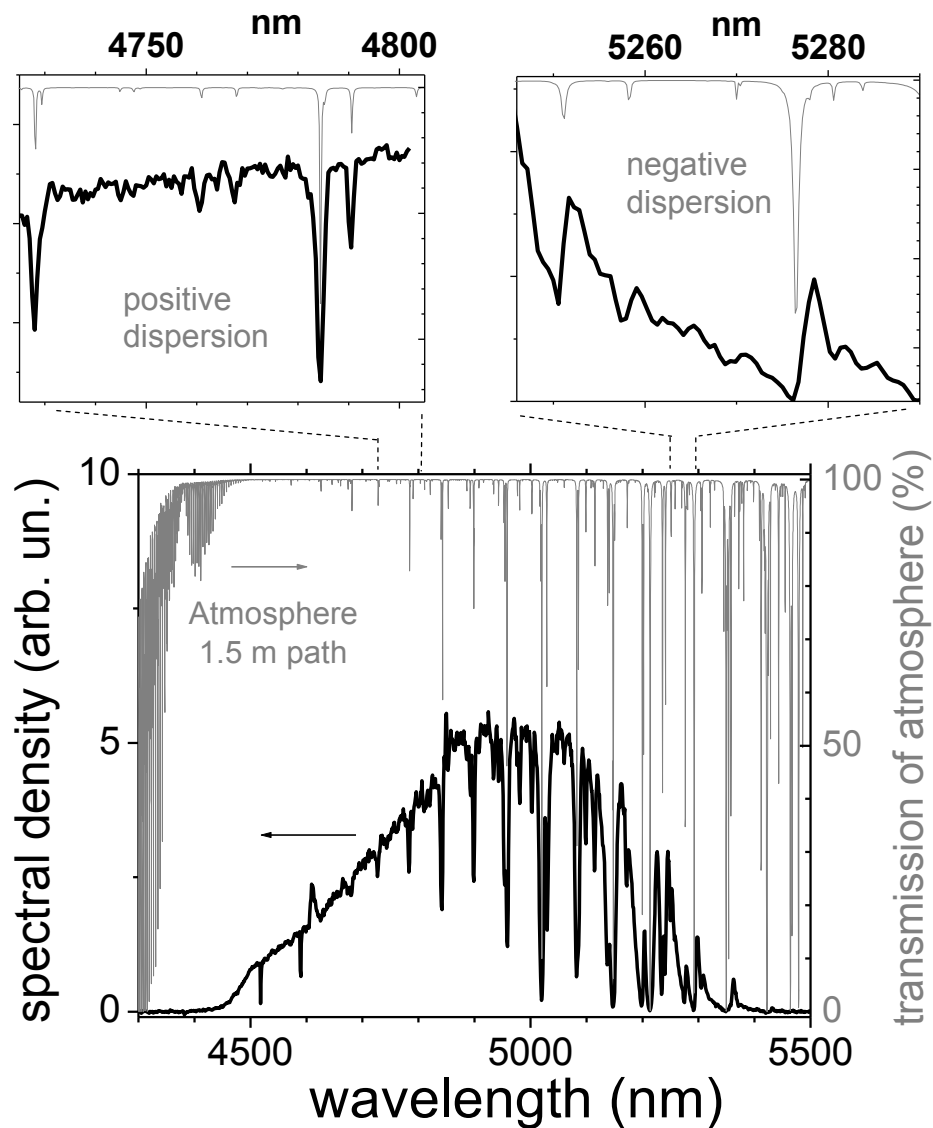




Results with orientation-patterned GaAs

Monochromator spectrum

The spectrum is affected by intracavity absorption (water and CO₂)





Most recently 3.5-5.5 μm frequency comb was produced in a subharmonic OP-GaAs OPO pumped by a femtosecond Tm^{3+} - fiber laser at $\lambda=2 \mu\text{m}$

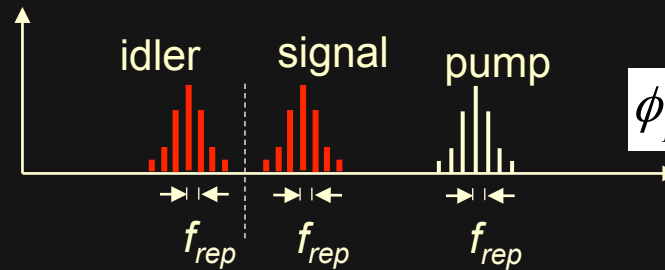


Coherence properties of divide-by-two OPO



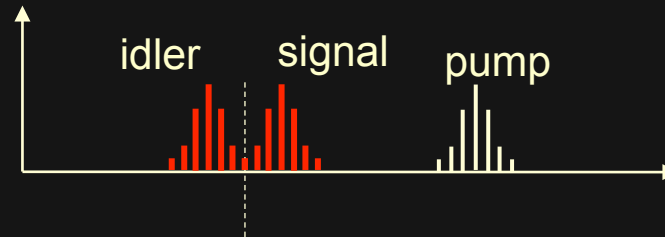
Divide-by-two synch-pumped OPO

non-degenerate
OPO



$$\phi_p = \phi_s + \phi_i + \pi / 2$$

partly
degenerate
OPO



degenerate
(divide-by-two)
OPO

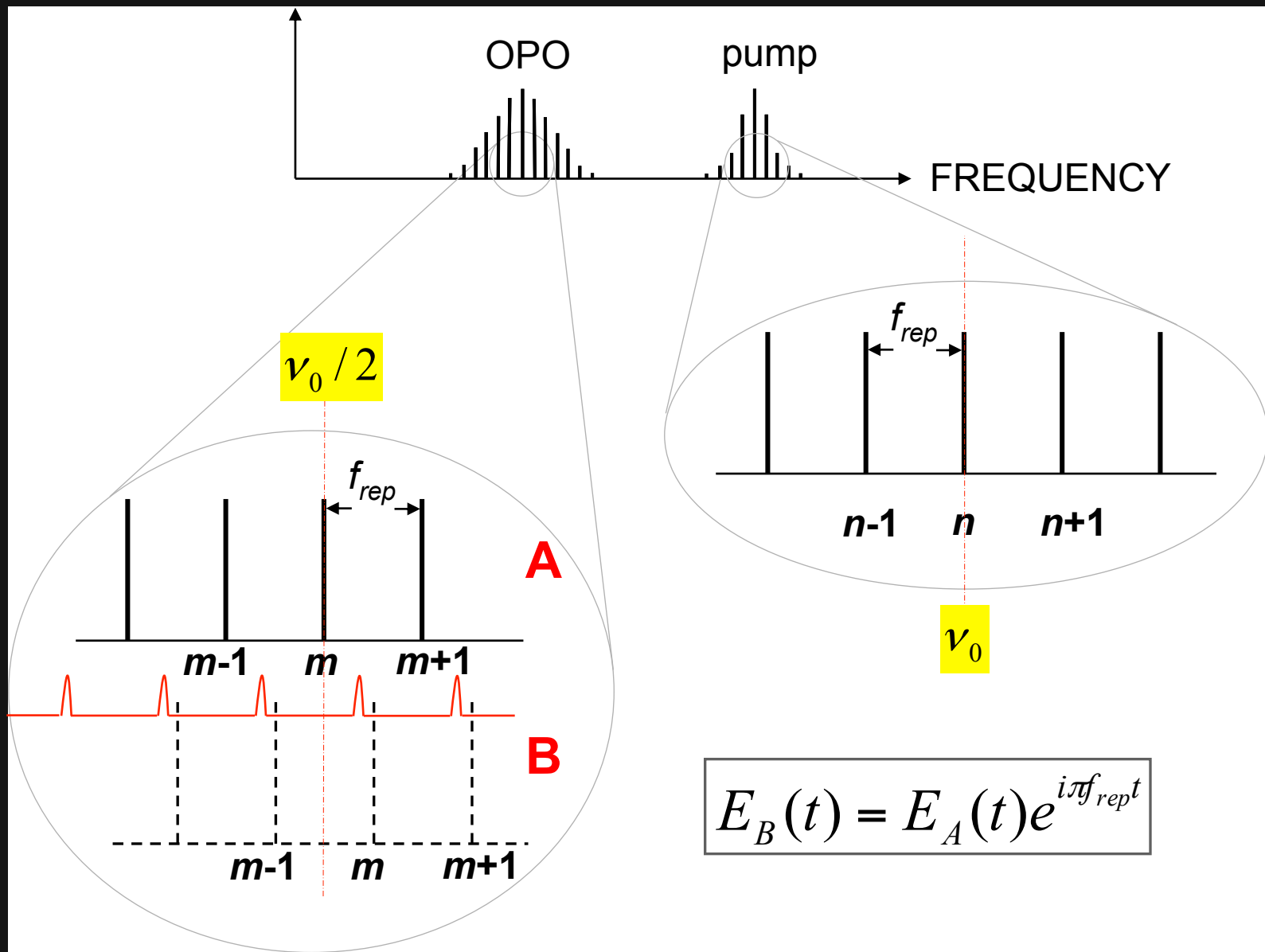


$$\phi_p = 2\phi_{s,i} + \pi / 2$$

- OPO is phase locked to the pump laser
- adding π to the signal and idler does not change phase relation



Longitudinal modes of the sync-pumped degenerate OPO

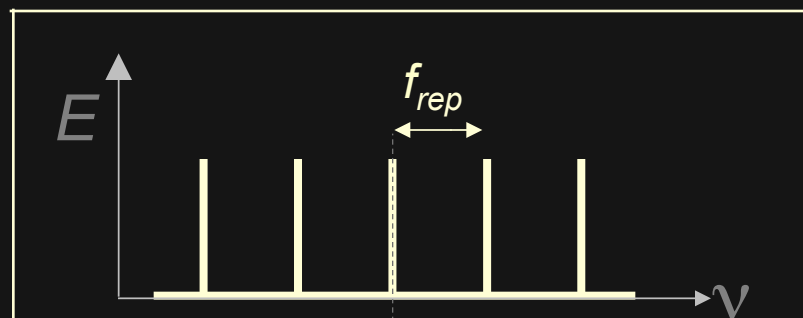




Four possibilities for the OPO mode phases

$$\phi=0$$

A



B

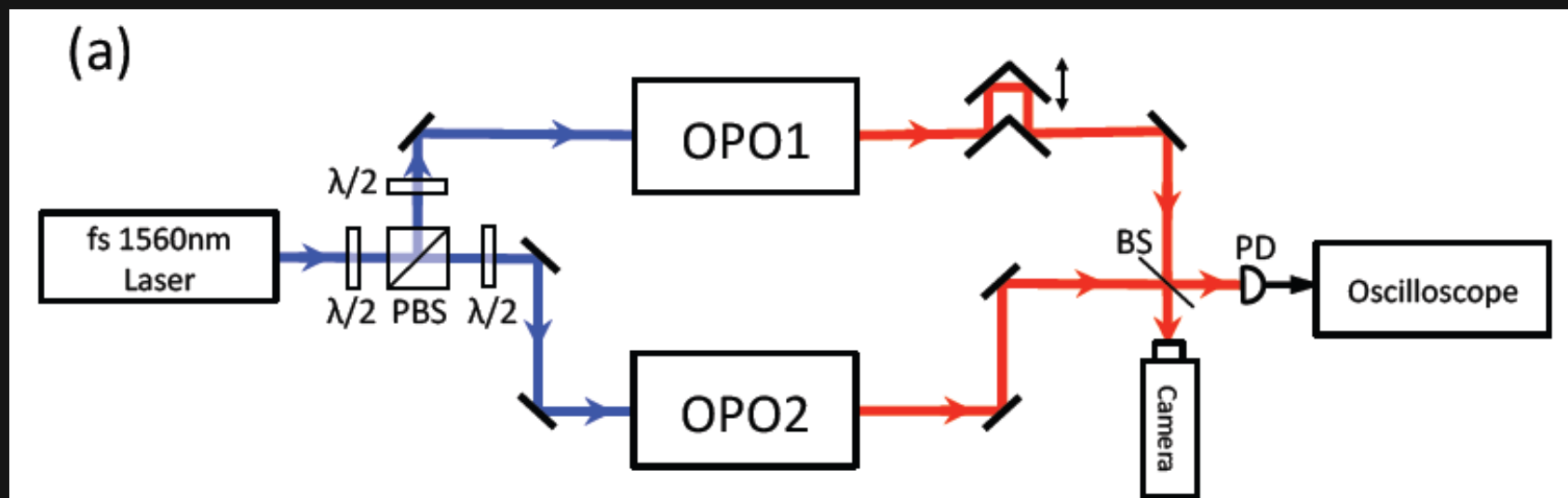




Experiment



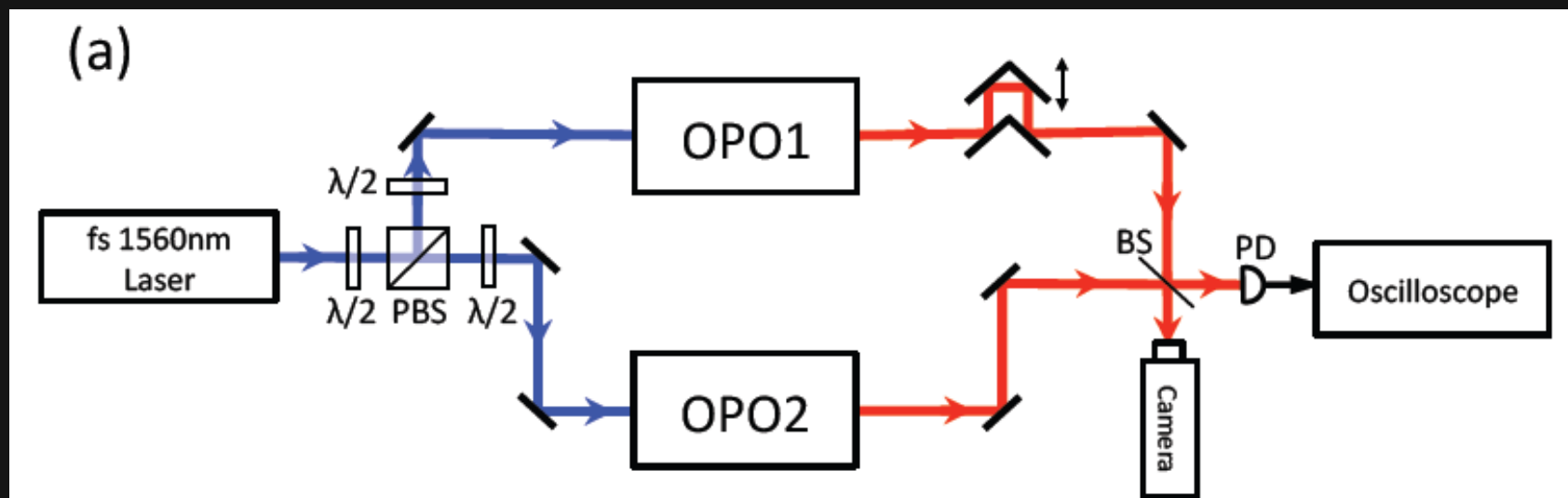
A twin OPO system



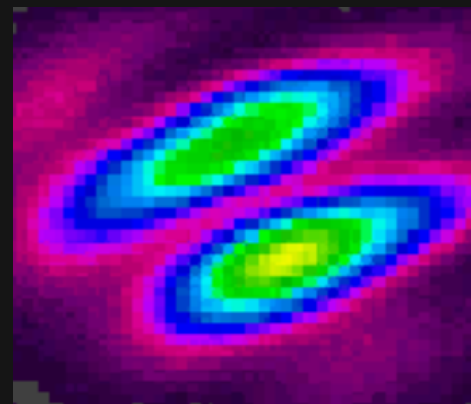
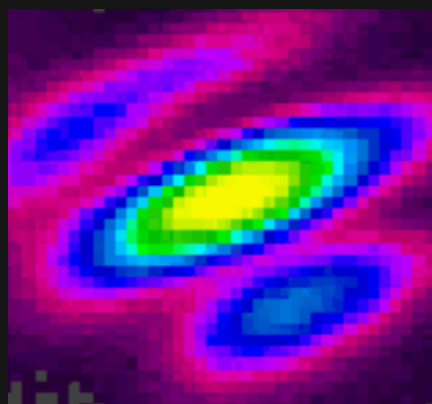
- 1) **AA or BB**
interfere constructively or destructively,
depending on the “0” or “ π ” state
- 2) **AB or BA**
do not interfere, but give $f_{\text{rep}}/2$ (50 MHz) beats



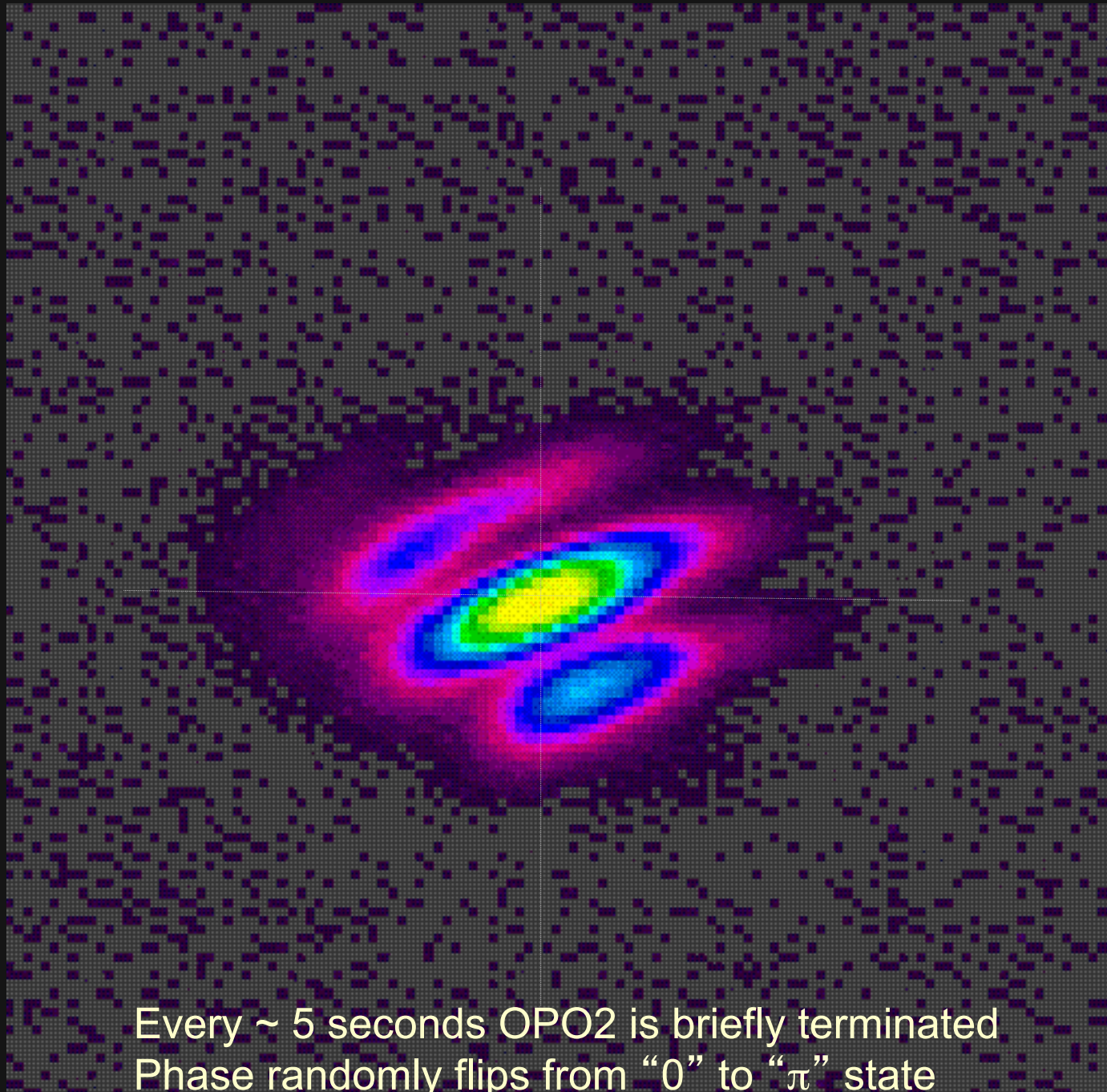
A twin OPO system



AA
or
BB

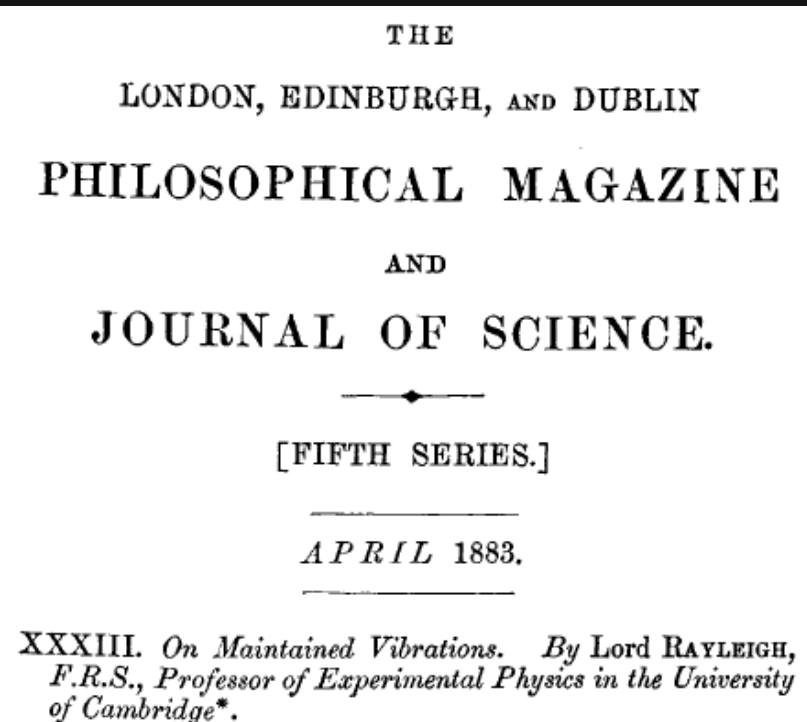
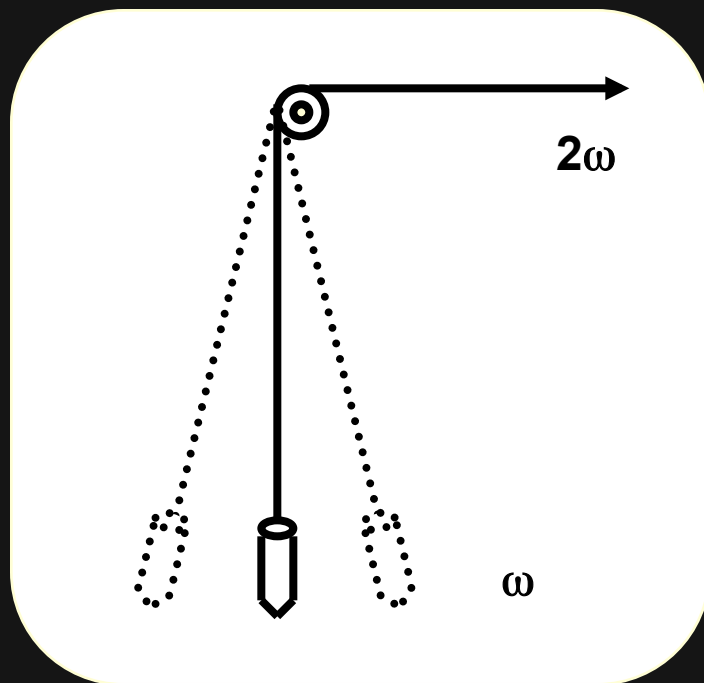


Observed spatial interference patterns





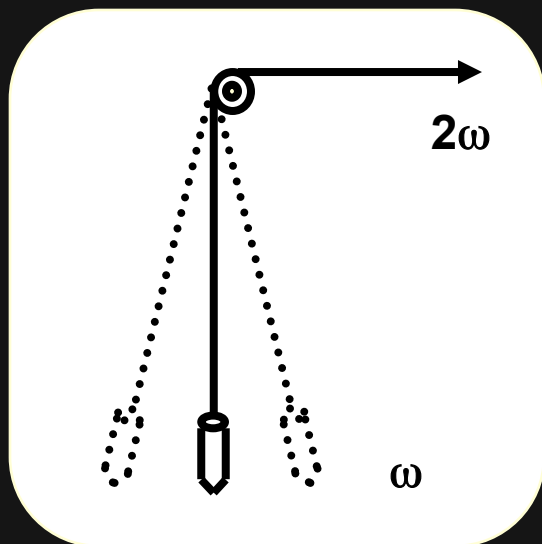
Mechanical analogy: parametrically driven pendulum



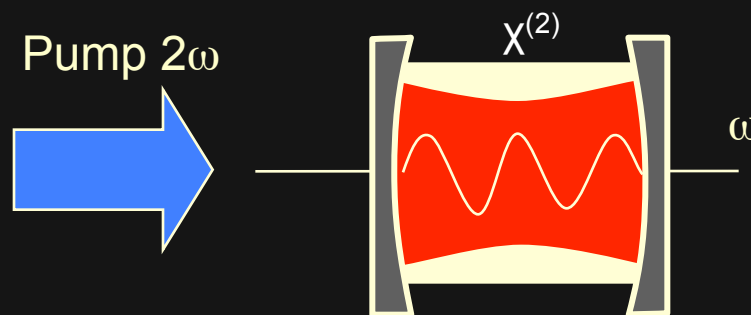
$$\ddot{\theta} + \omega^2 (1 - 2\alpha \sin 2\omega t) \theta = 0$$



Mechanical and optical parametric oscillators are described by the same equation



$$\ddot{\theta} + \omega^2 (1 - \alpha \sin 2\omega t) \theta = 0$$



E-field in a cavity mode:

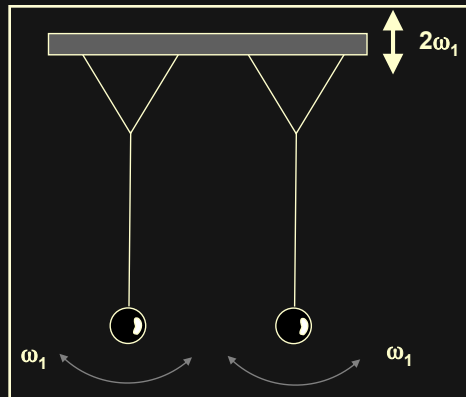
$$E(\mathbf{r}, t) = p_l(t) E_l(\mathbf{r})$$

$$\ddot{p}_l + \omega^2 p_l = 0; \quad \omega = \frac{k_l}{\sqrt{\mu \epsilon}}$$

$$\Delta \epsilon \sim \chi^{(2)} E_{pump}$$



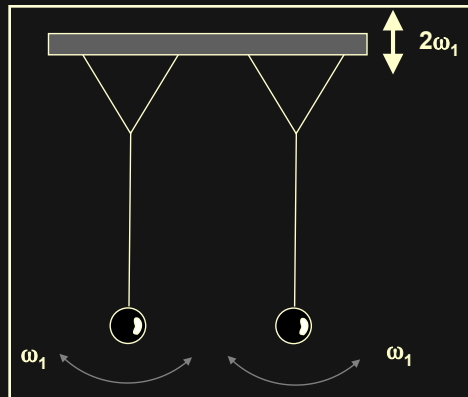
Mechanical analogy: parametrically driven pendulum



Two independent parametrically driven pendulums
start randomly in-phase or out-of-phase



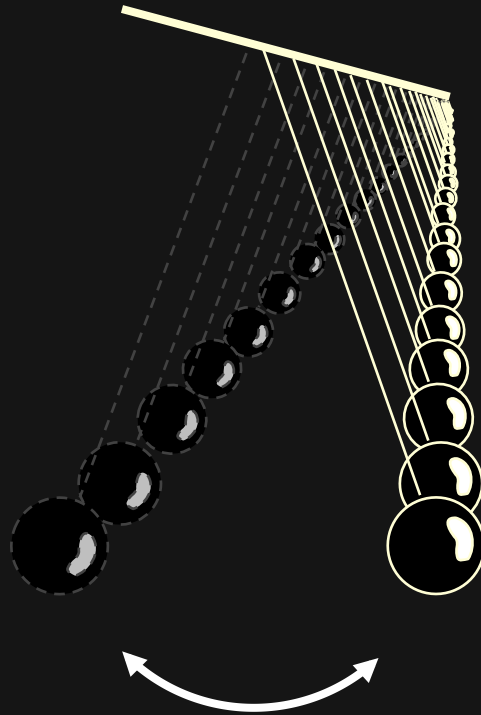
Mechanical analogy: parametrically driven pendulum



Two independent parametrically driven pendulums
start randomly in-phase or out-of-phase



300 000 oscillators in phase

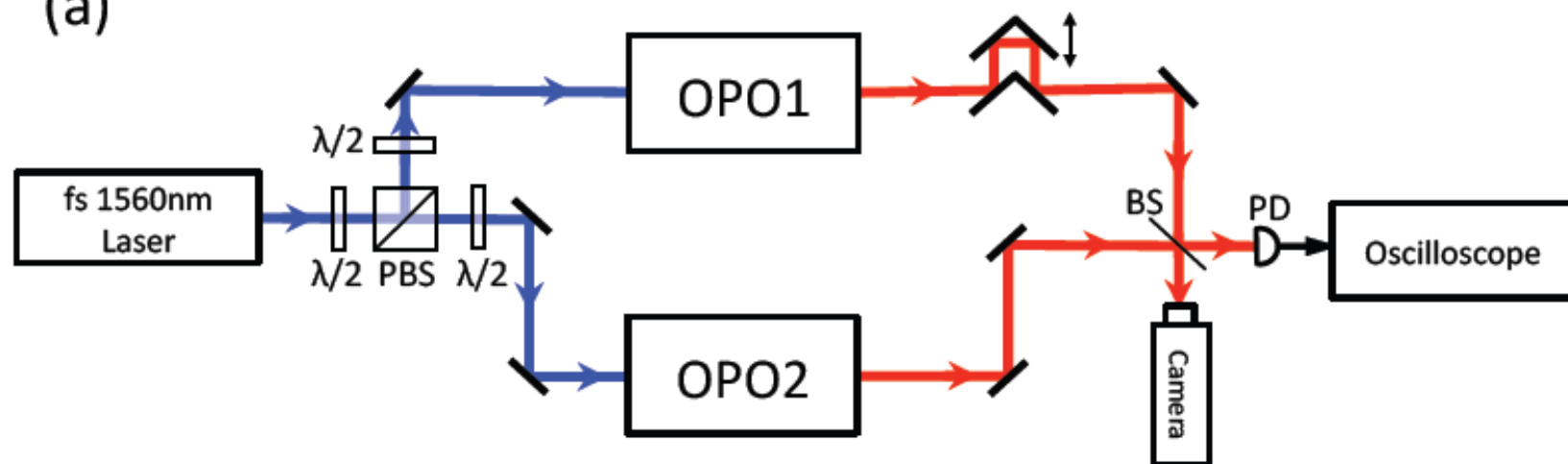


Some 300 000
pendulums oscillate
with the same
phase “0” or “ π ”



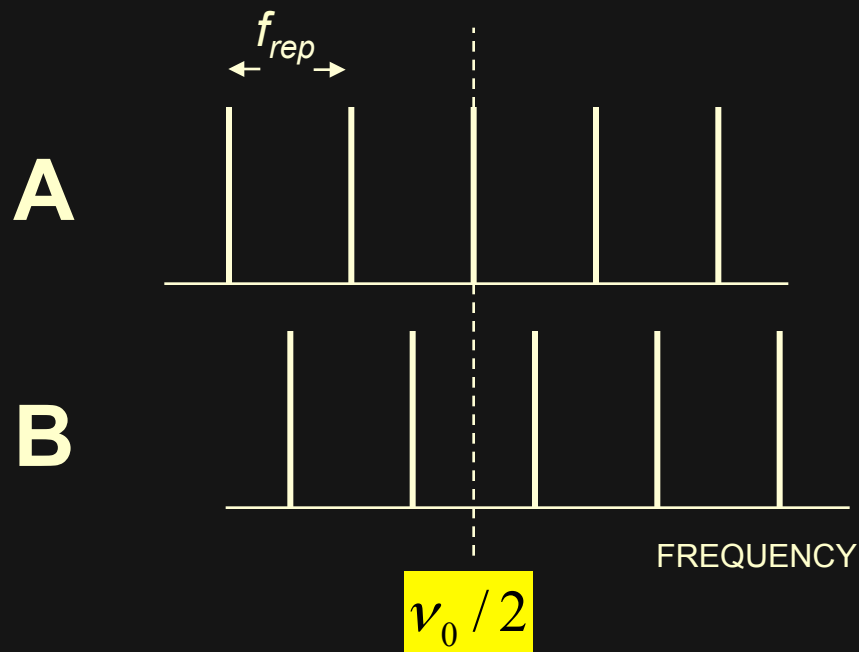
A twin OPO system: beat note study

(a)





Two possible states: 'odd' and 'even'

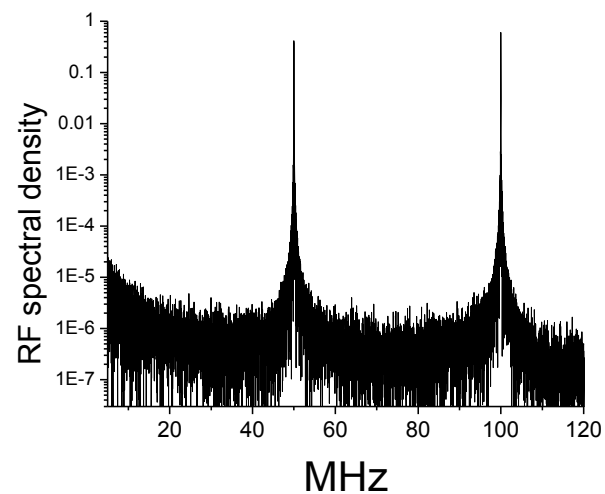
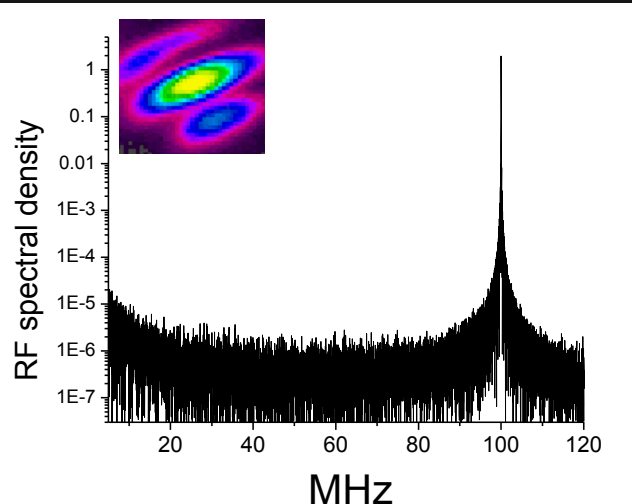


**Switching between A and B is totally deterministic !
(by adjusting cavity length)**

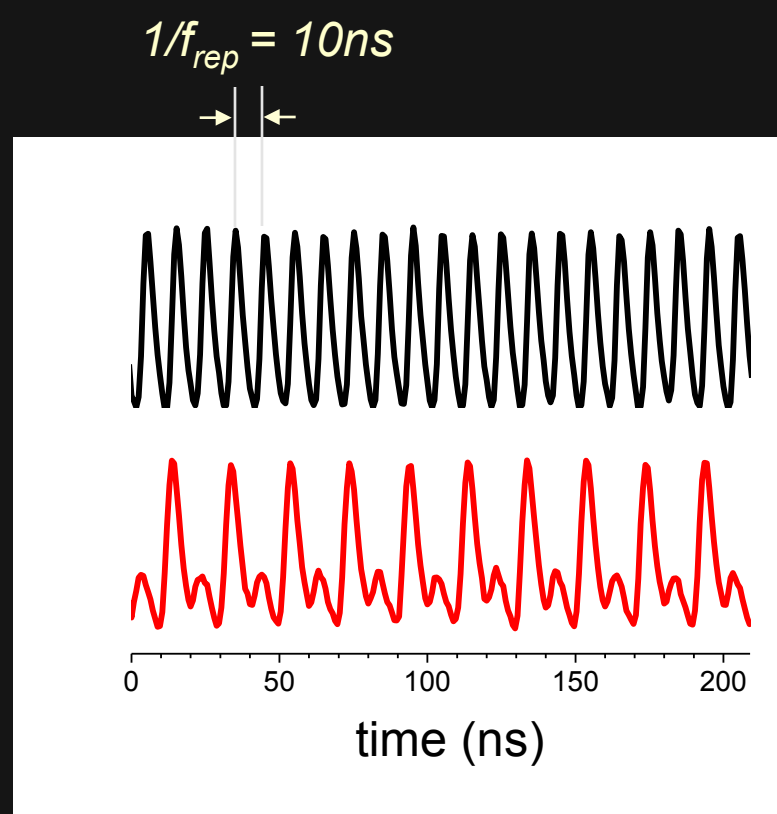


Observation of beats at $f_{\text{rep}}/2$

RF spectrum

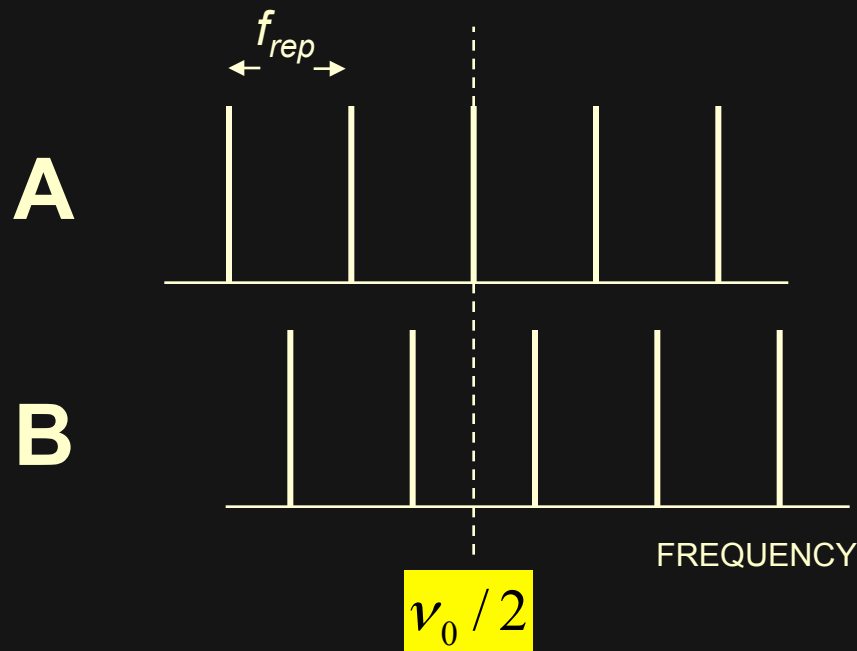


Time-domain signal





Two possible states: 'odd' and 'even'



$$E_B(t) = E_A(t)e^{i2\pi\frac{f_{rep}}{2}t}$$

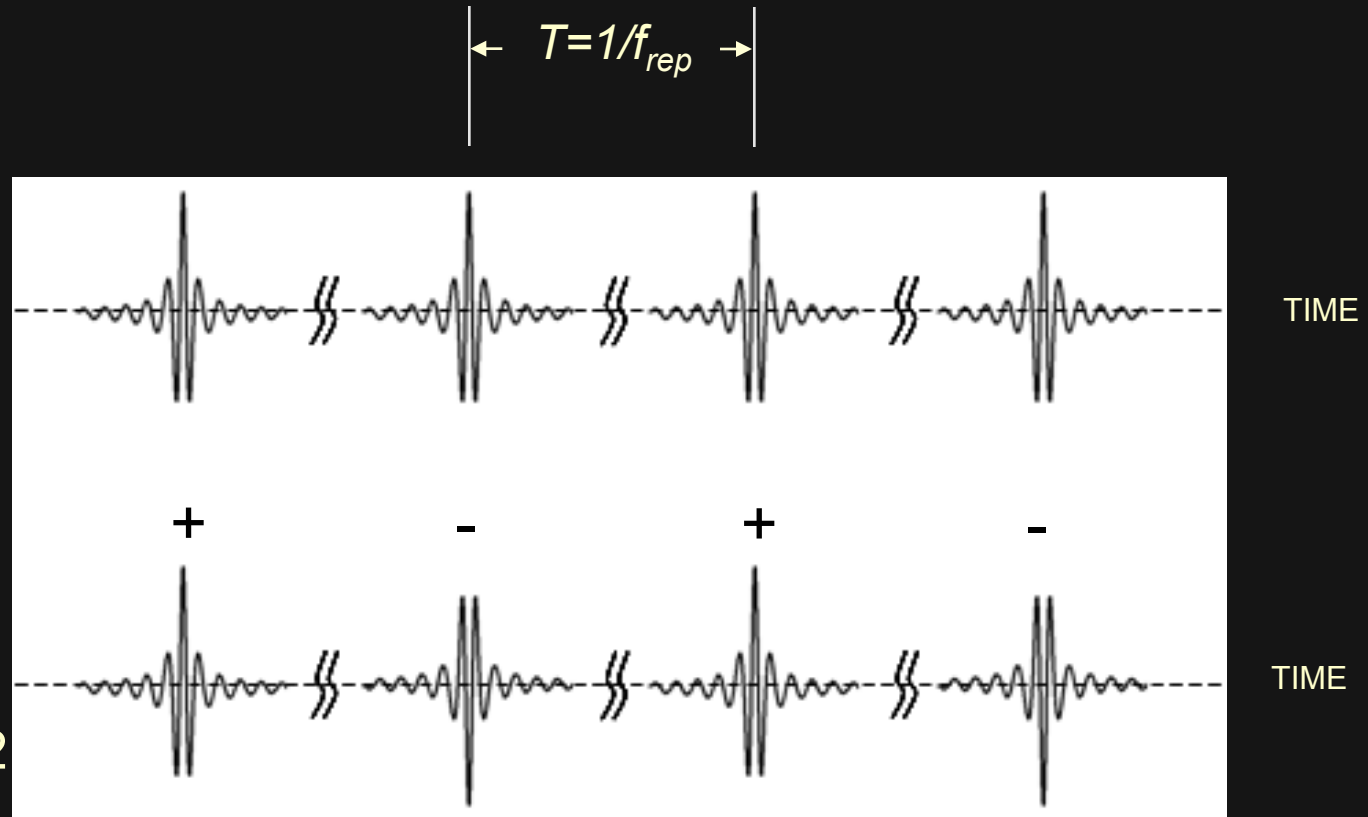
**Switching between A and B is totally deterministic !
(adjust cavity length)**



In time domain

A
 $f_{\text{ceo}} = 0$

B
 $f_{\text{ceo}} = f_{\text{rep}}/2$



$$E_B(t) = E_A(t)e^{i\pi f_{\text{rep}} t}$$

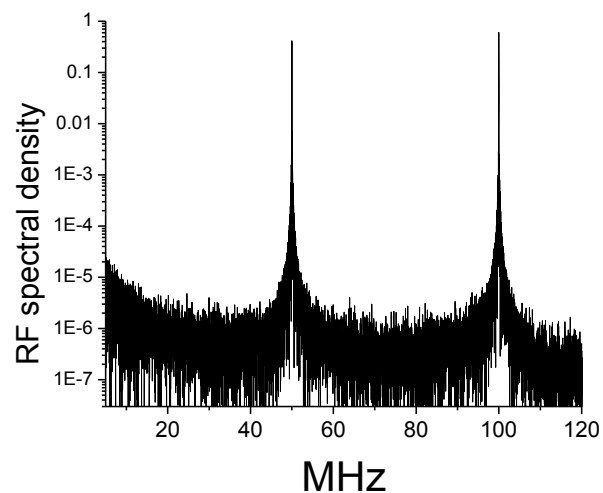
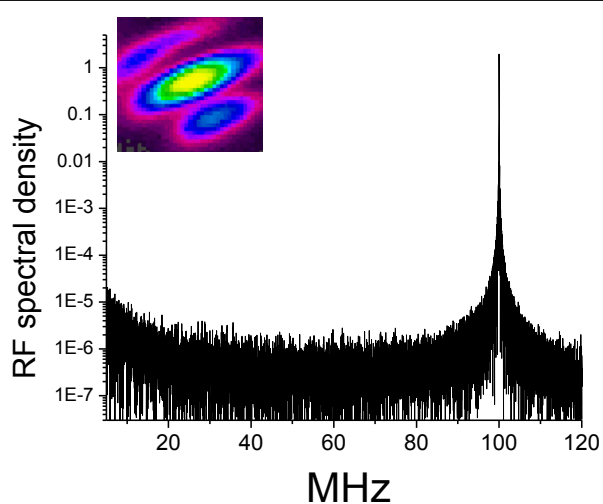
$$e^{i\pi f_{\text{rep}} t} = 1 \quad \text{for even pulses}$$

$$e^{i\pi f_{\text{rep}} t} = -1 \quad \text{for odd pulses}$$

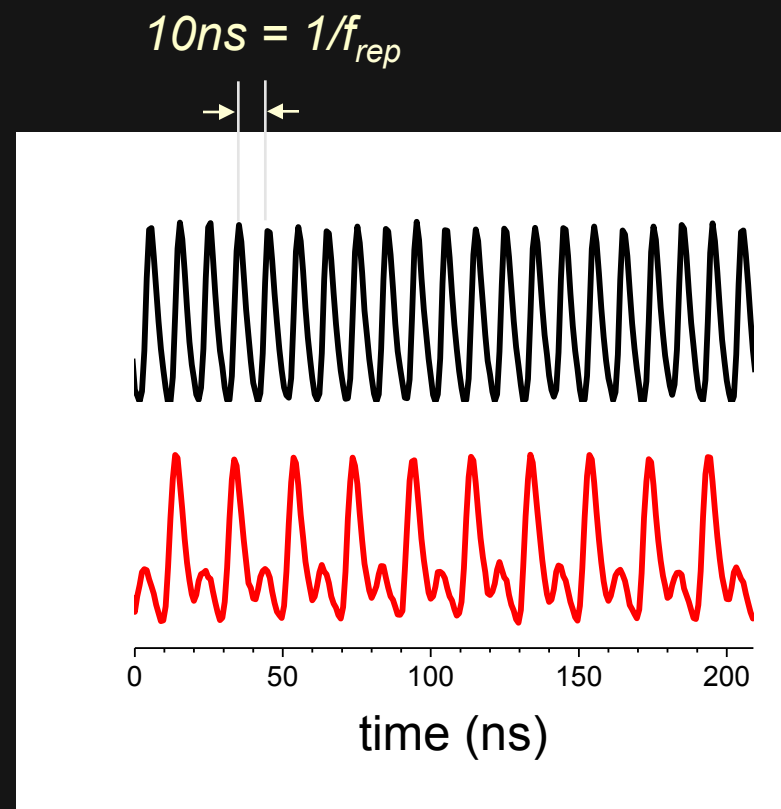


Observation of beats at $f_{\text{rep}}/2$

RF spectrum

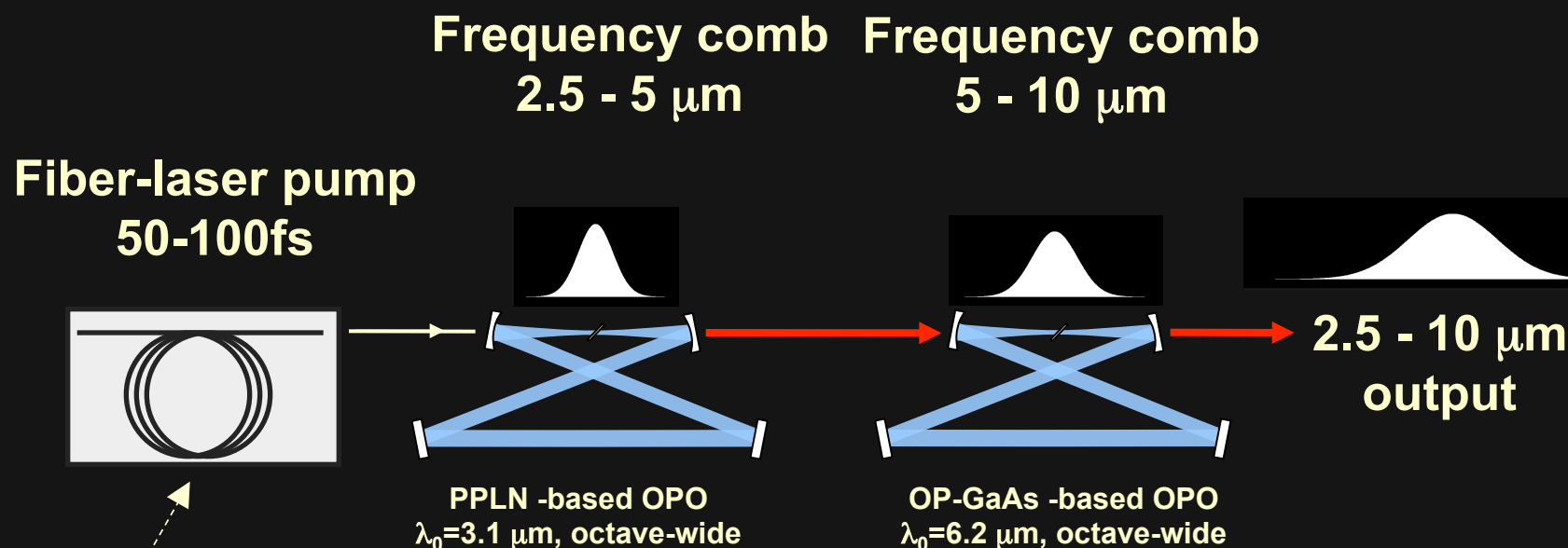


Time-domain signal





Divide-and-conquer approach: ultimate concept of a cascaded OPO setup



Broad-bandwidth (2.5 - 10 μm) mid-IR frequency comb
source consisting of two consecutive subharmonic OPOs.

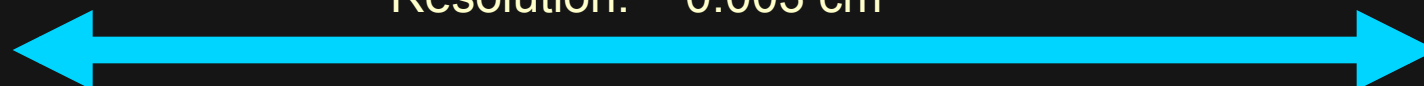
Nonlinear crystals can be ~ one coherence length long !



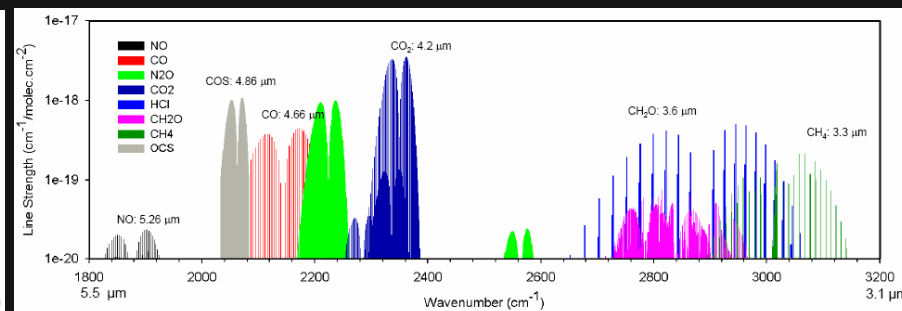
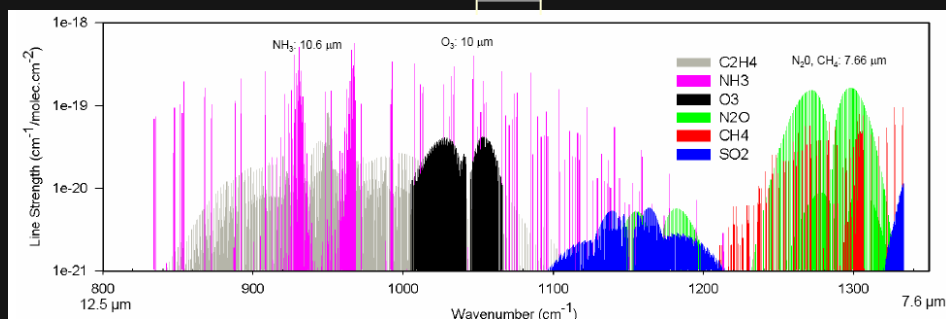


Desired mid-IR comb spectral coverage

Frequency comb spectral coverage: 2 octaves
Resolution: $\sim 0.003 \text{ cm}^{-1}$



QCL tuning range



12.5 μm

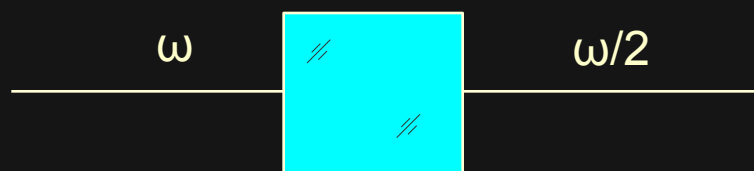
$\lambda = 7.6 \mu\text{m}$ 5.5 μm

3 μm

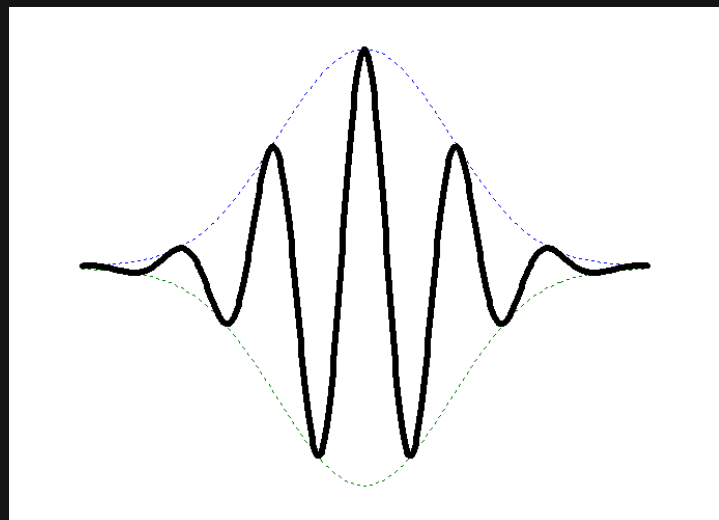


Is the assumption that pulses consist of modes necessary ?

Implementation for the single pass subharmonic generation

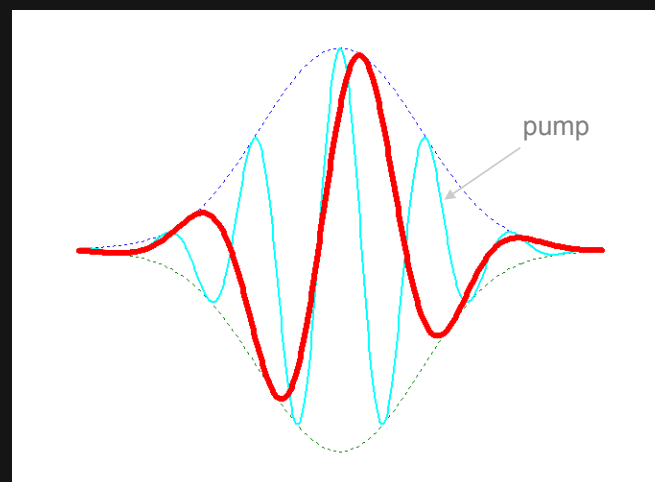


Pump

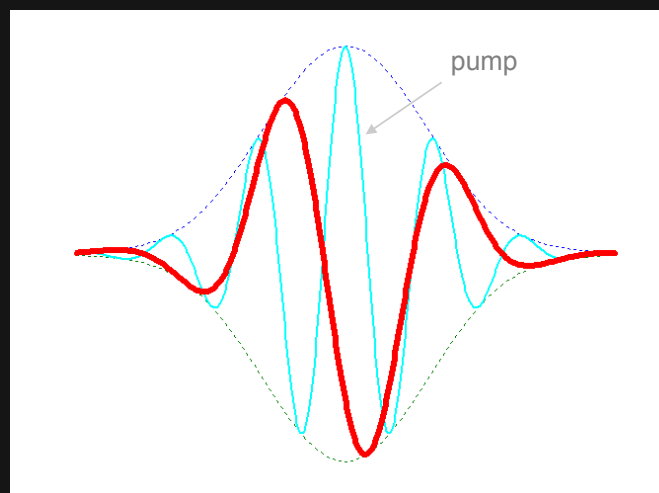


$$\sqrt{1} = \pm 1$$

Subharmonic



0 -state



π -state

Conclusion



- ‘Frequency-divide-by-two’ approach allows to jump right into mid-IR region and broaden the pump comb
- 9 mW threshold, 60 mW output
- Wavelength span: close to an octave in the mid-IR
- Phase- and frequency locked to the pump, other interesting coherence properties
- Frequency comb coherence – inherited from the pump
- Applications: molecular spectroscopy, trace detection, quantum optics, random number generation ...

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